

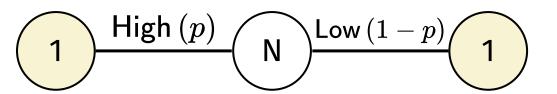
# REAL LIFE GAMES: HOW GAME THEORY SHAPES HUMAN DECISIONS

# SIGNALING GAMES

Adrian Haret
a.haretalmu.de

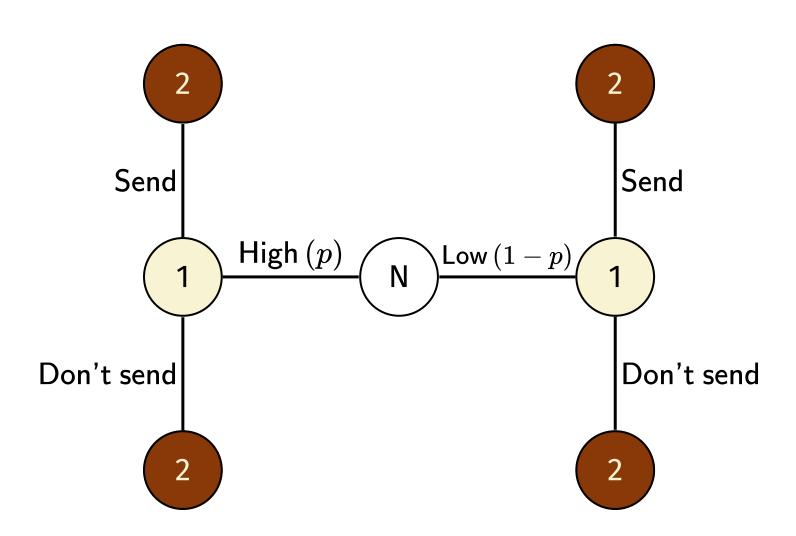
In signaling games players need to be screened based on public information (signals) about some private trait (type).

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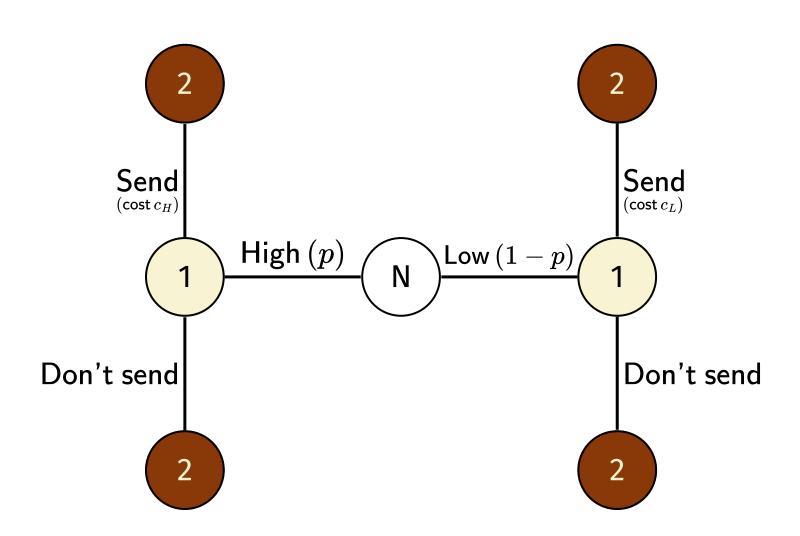
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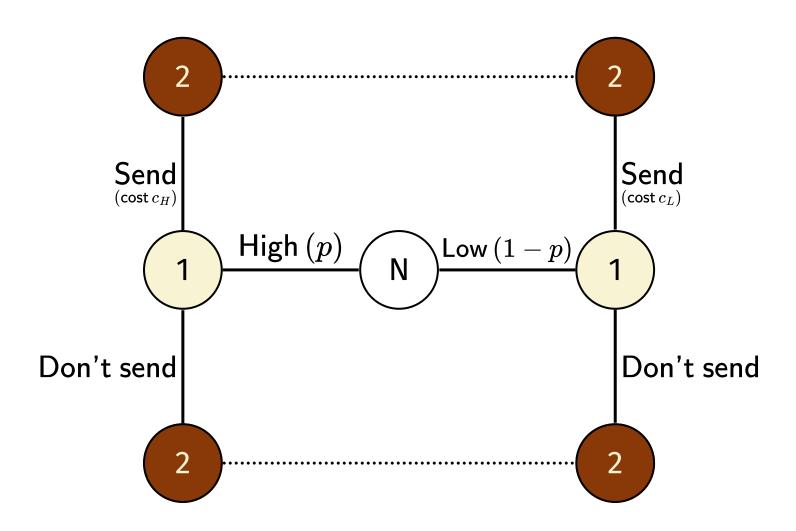


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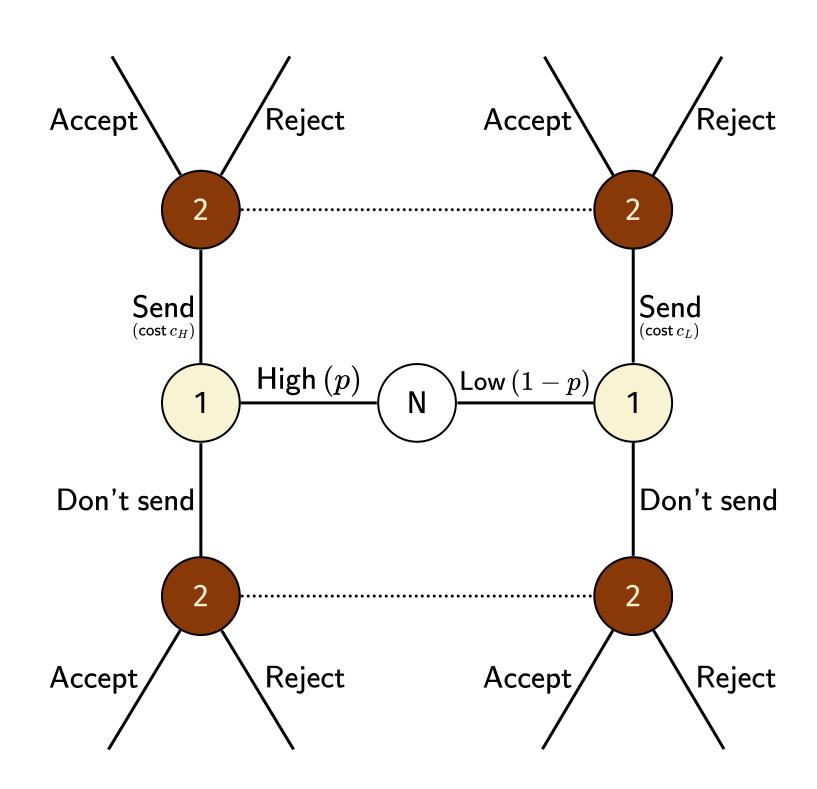
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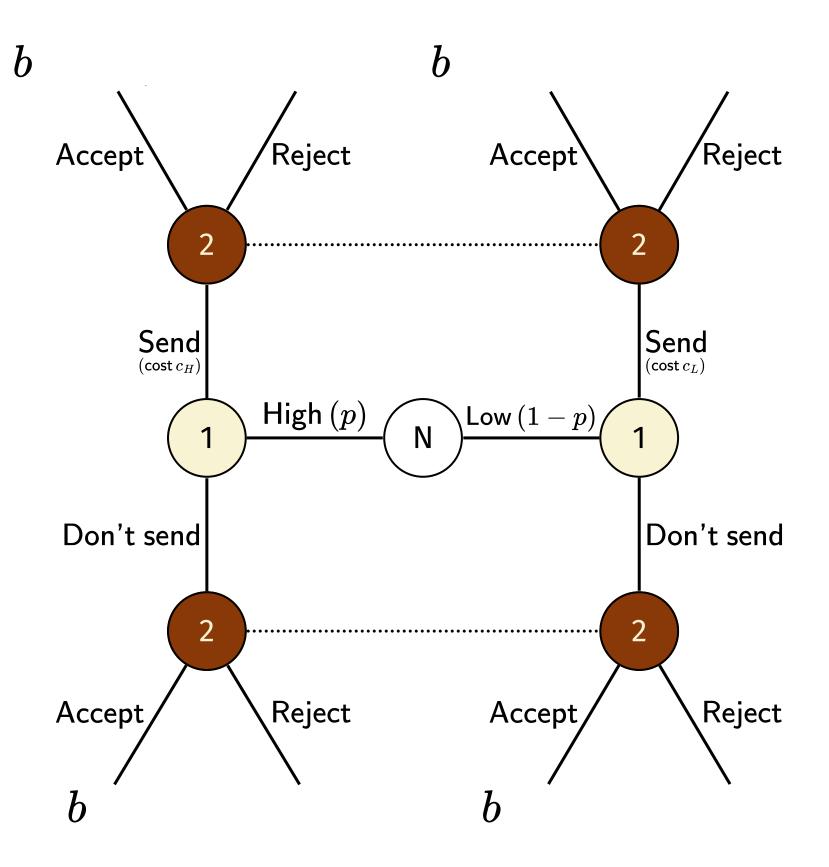
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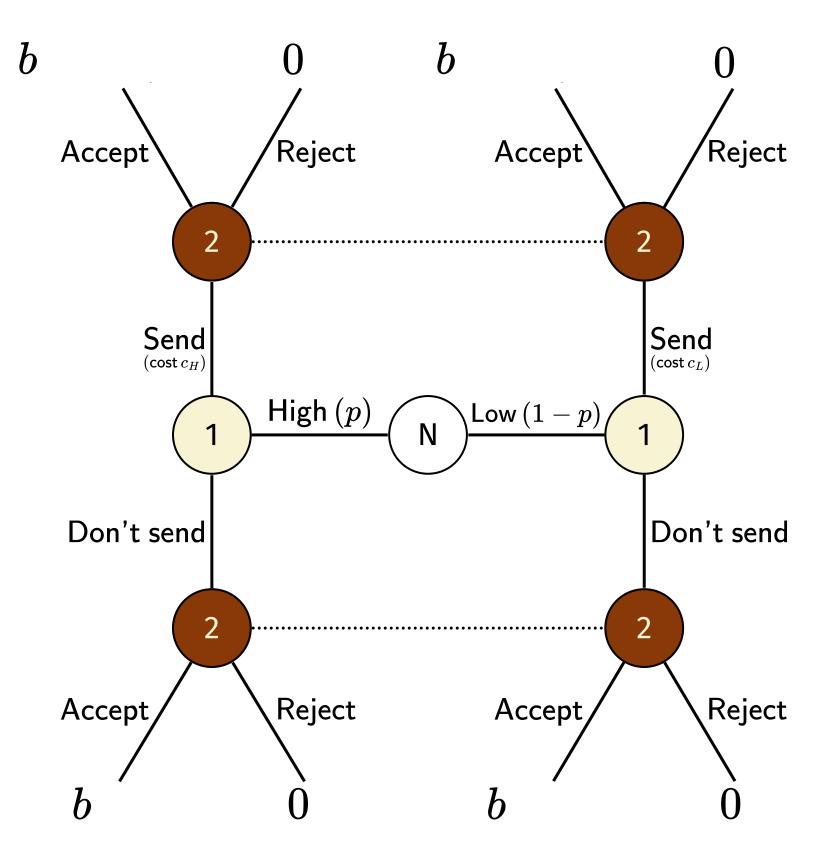
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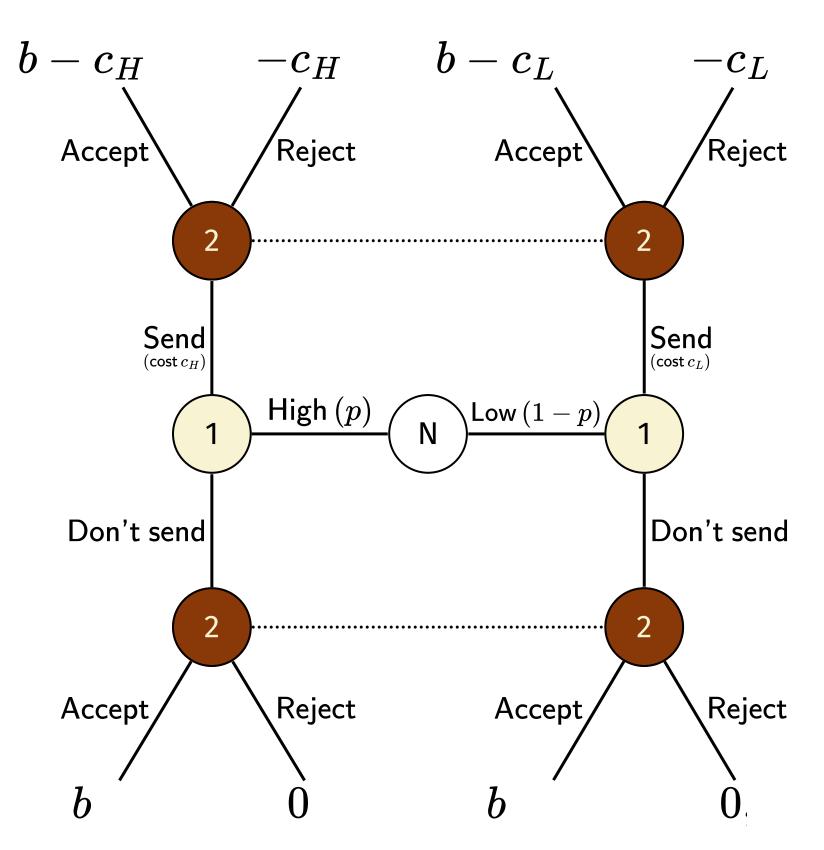
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Player 2 chooses to accept or reject Player 1.

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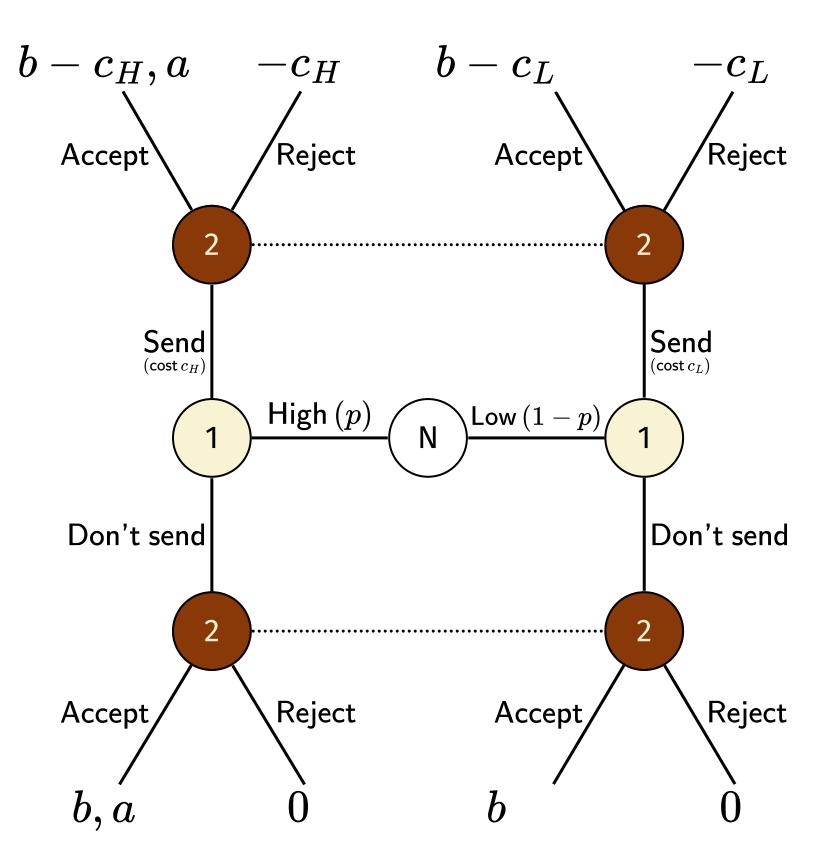
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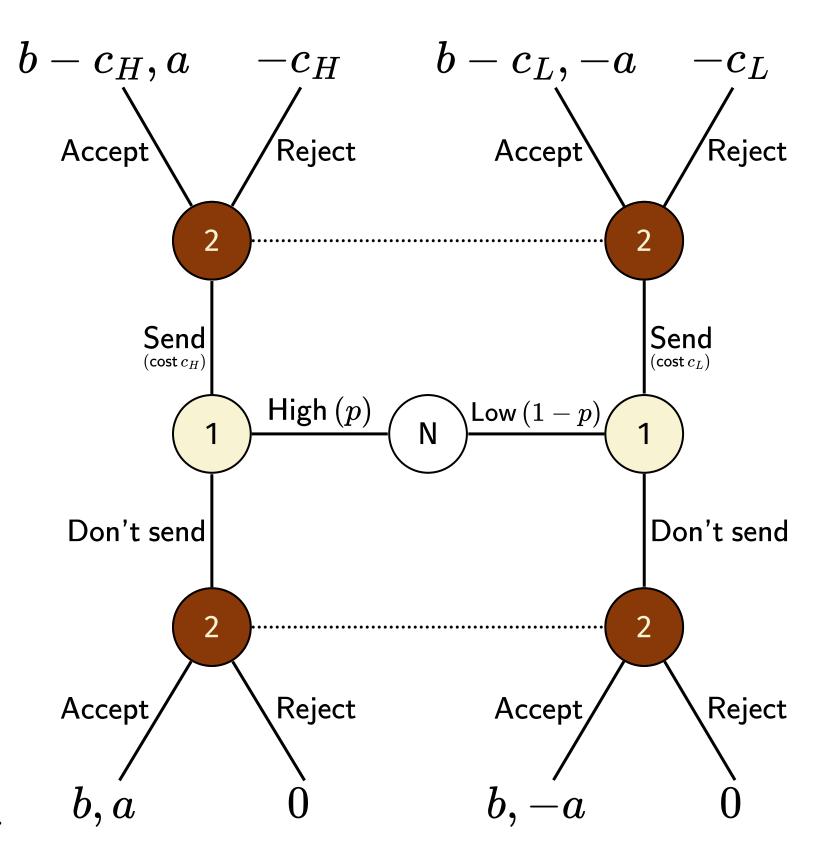
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\*Player 2 prefers to accept Player 1 only if they are a High type.



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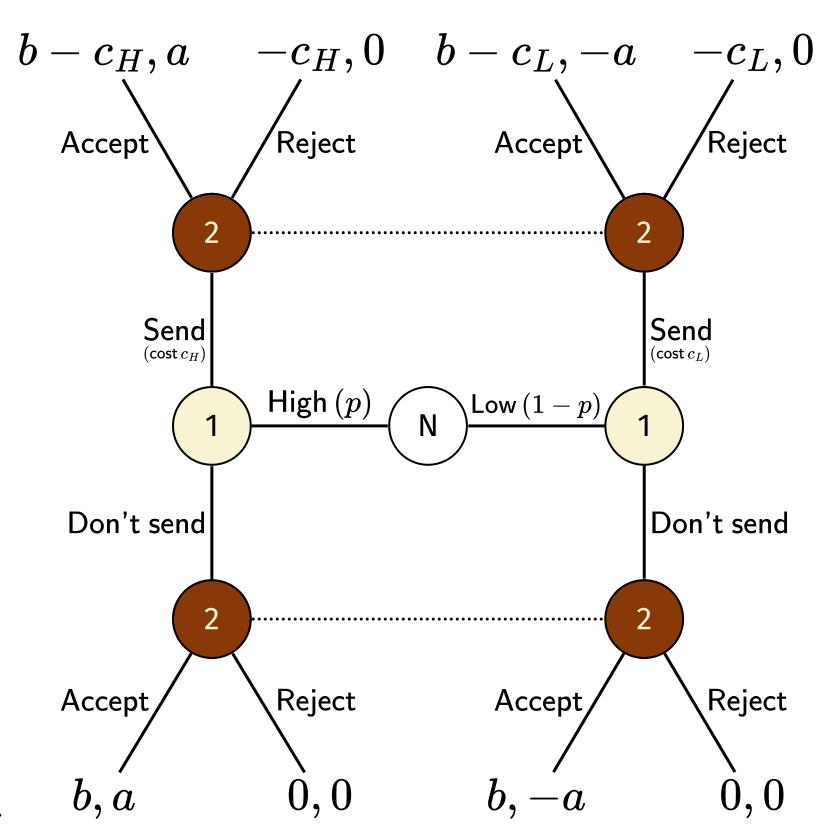
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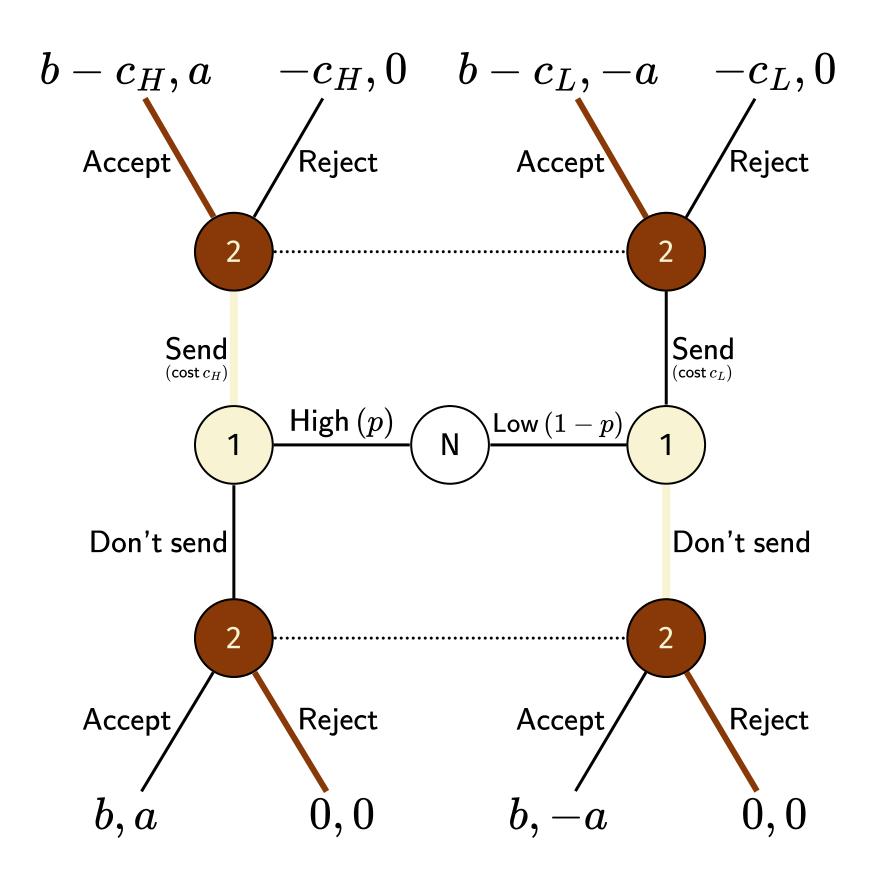


There can be different types of equilibria. We are interested here in separating equilibria.

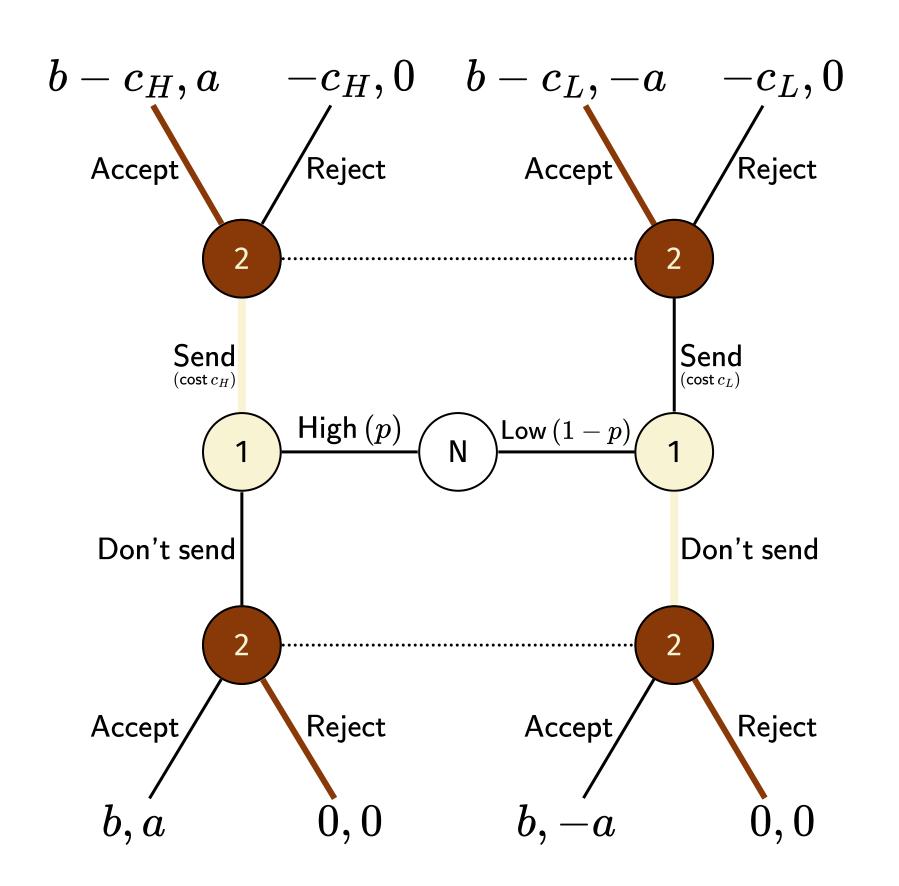
There can be different types of equilibria. We are interested here in *separating equilibria*. These are strategies where Player 1 signals only if they are of high type, and Player 2 accepts only if Player 1 sends the signal.

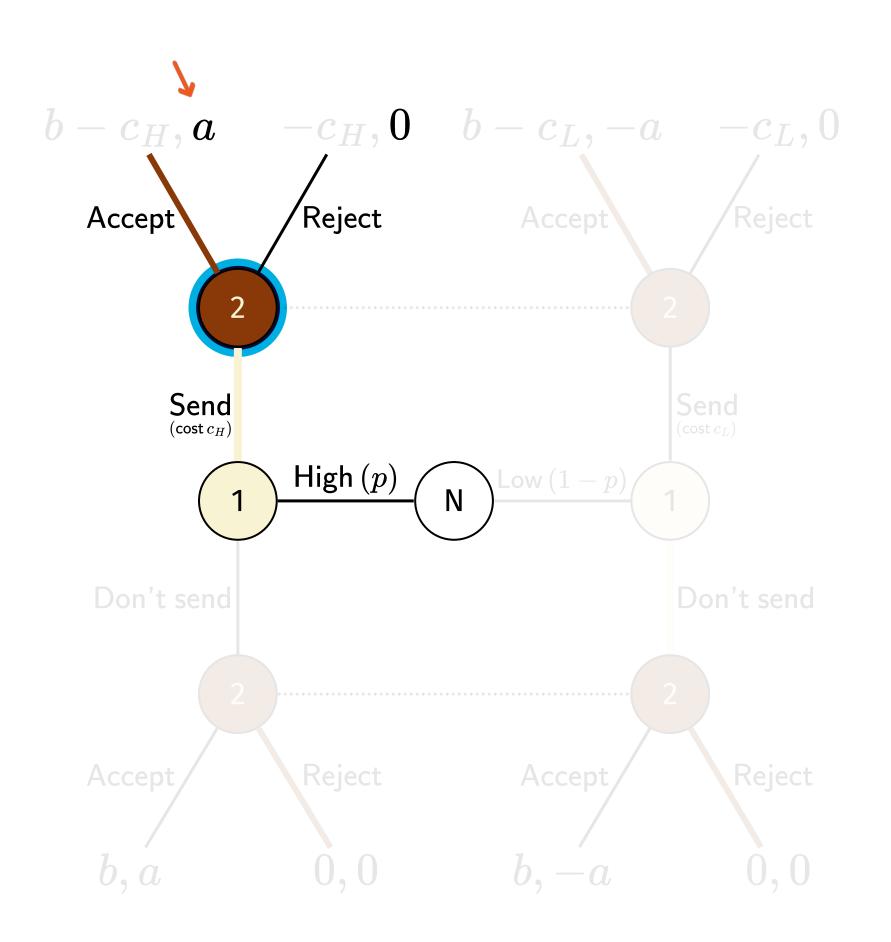
Player 1 sends the signal iff they are High type.

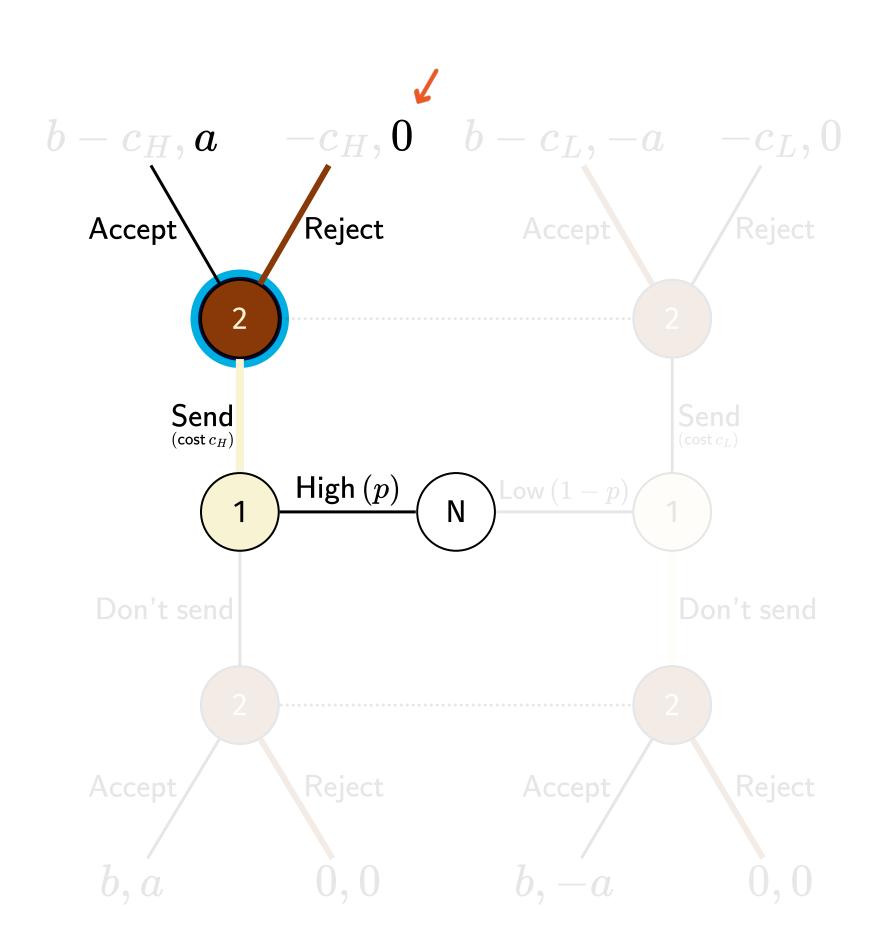
Player 2 accepts iff Player 1 sends the signal.

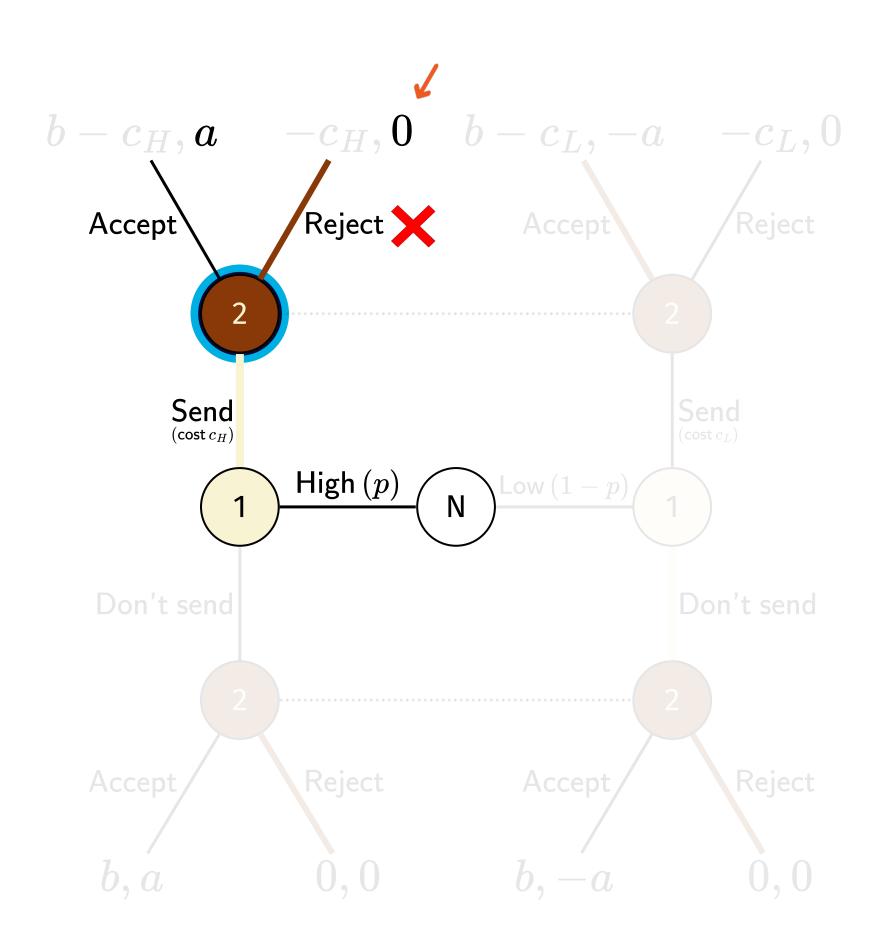


Is this an equilibrium? We have to check for deviations!

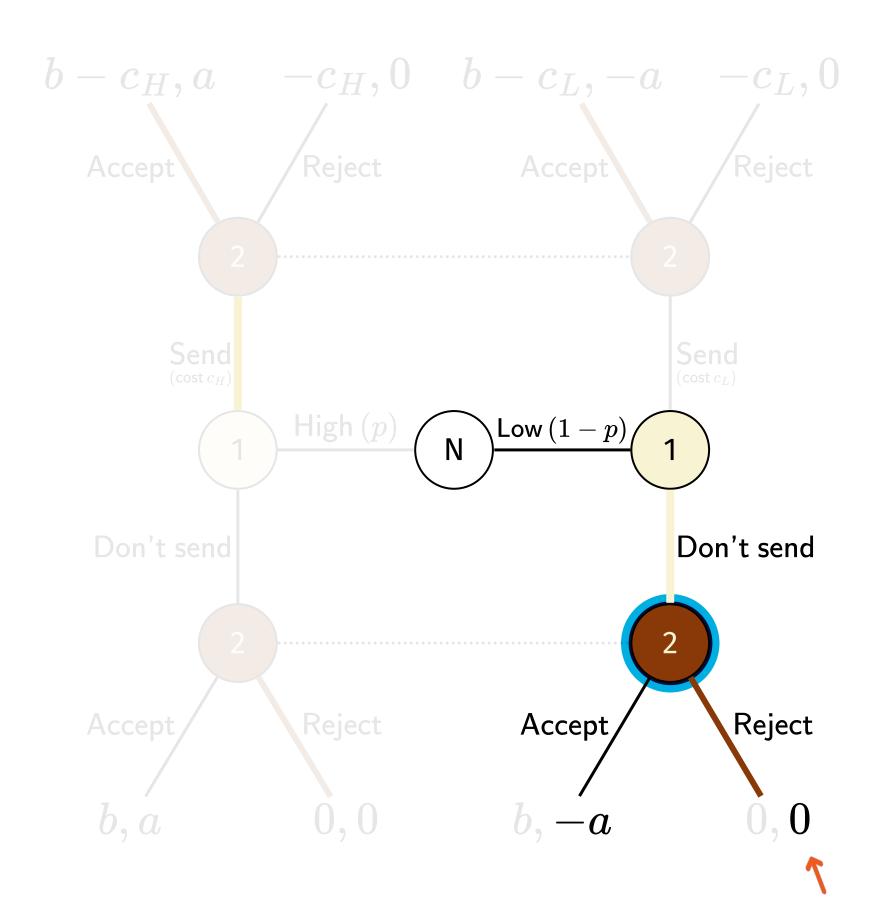




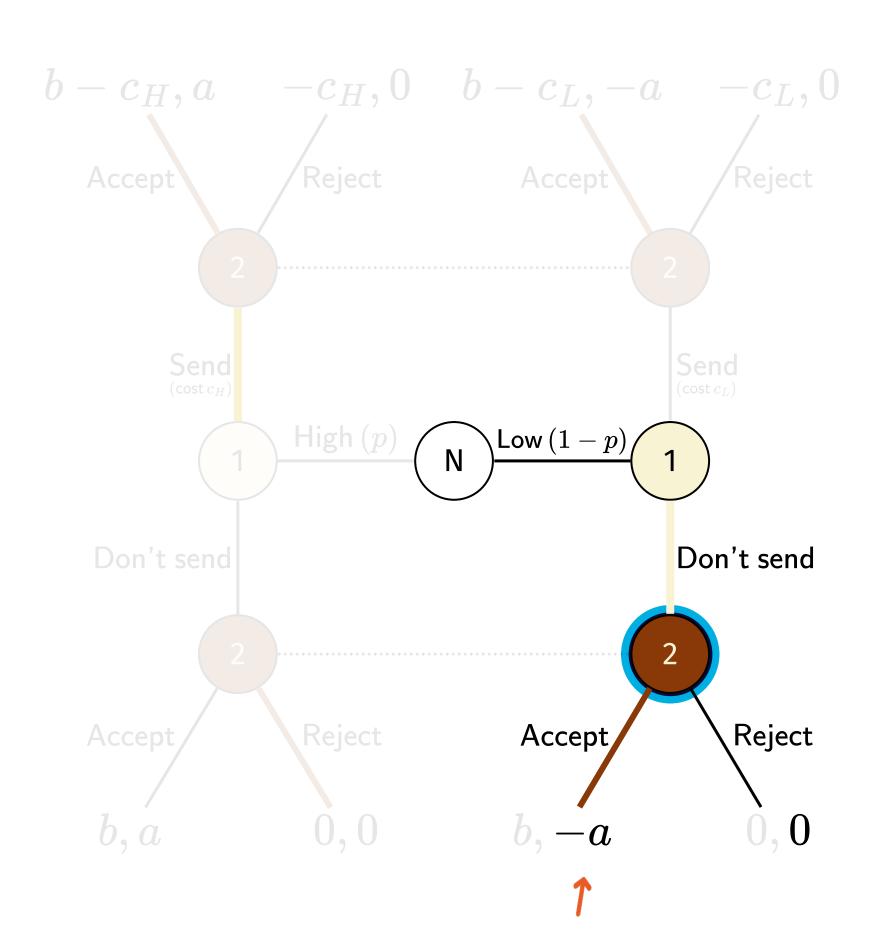




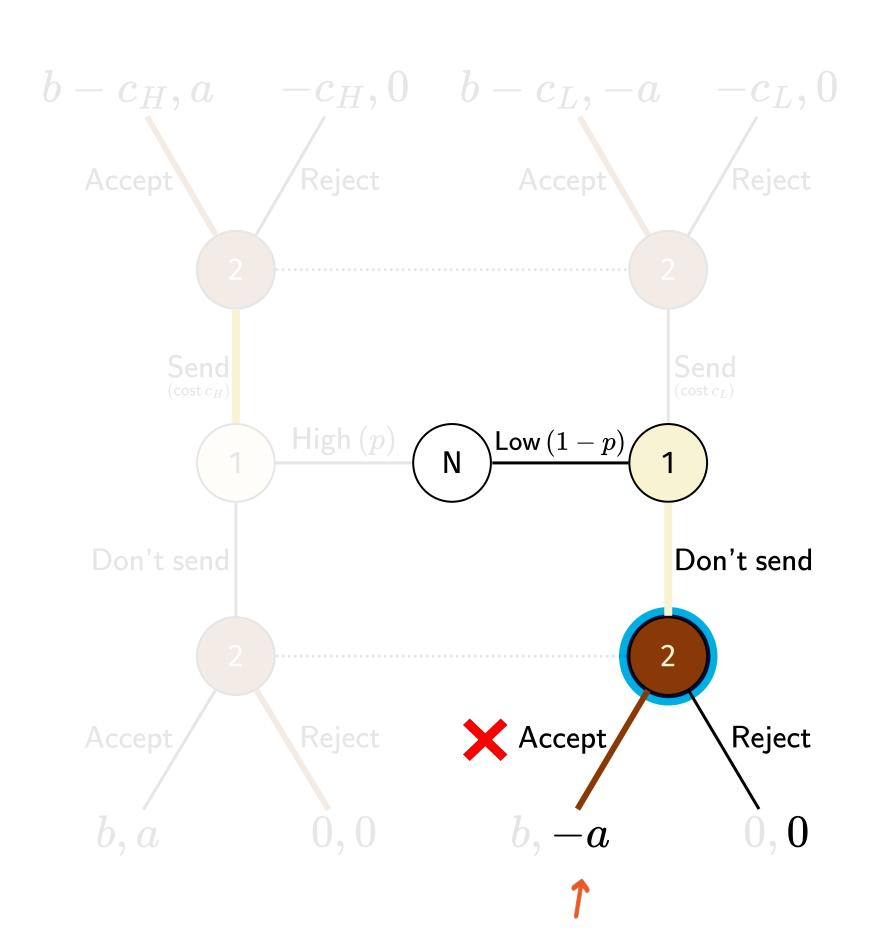
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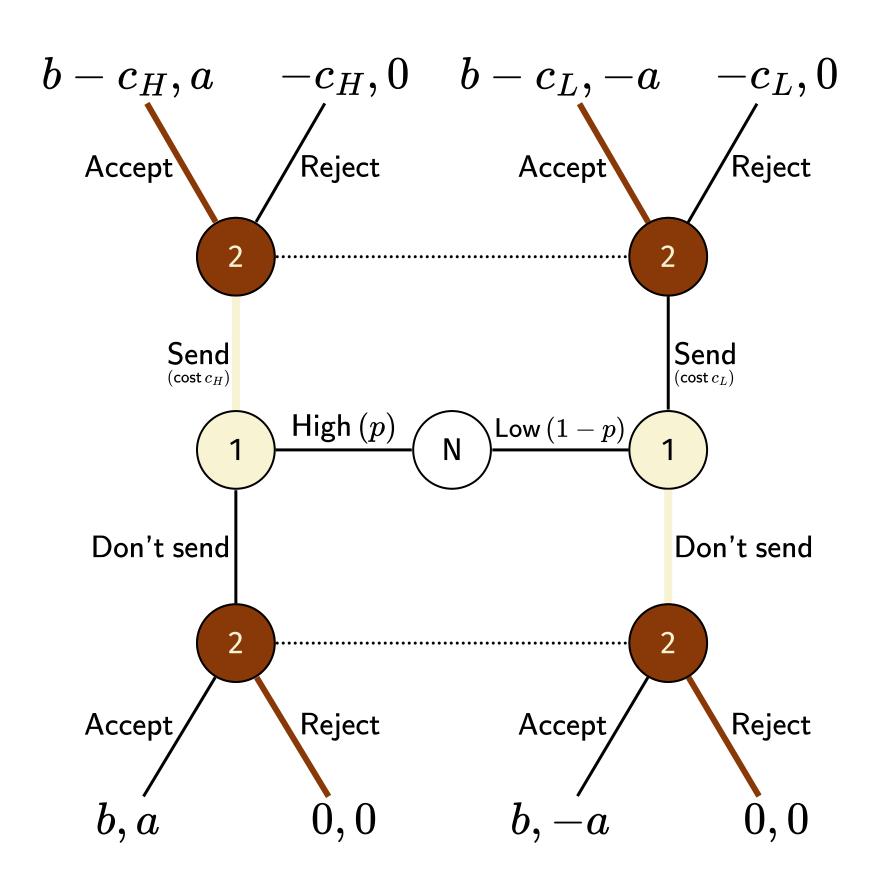
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Keeping Player 1's strategy fixed, Player 2 does not want to deviate just in case:

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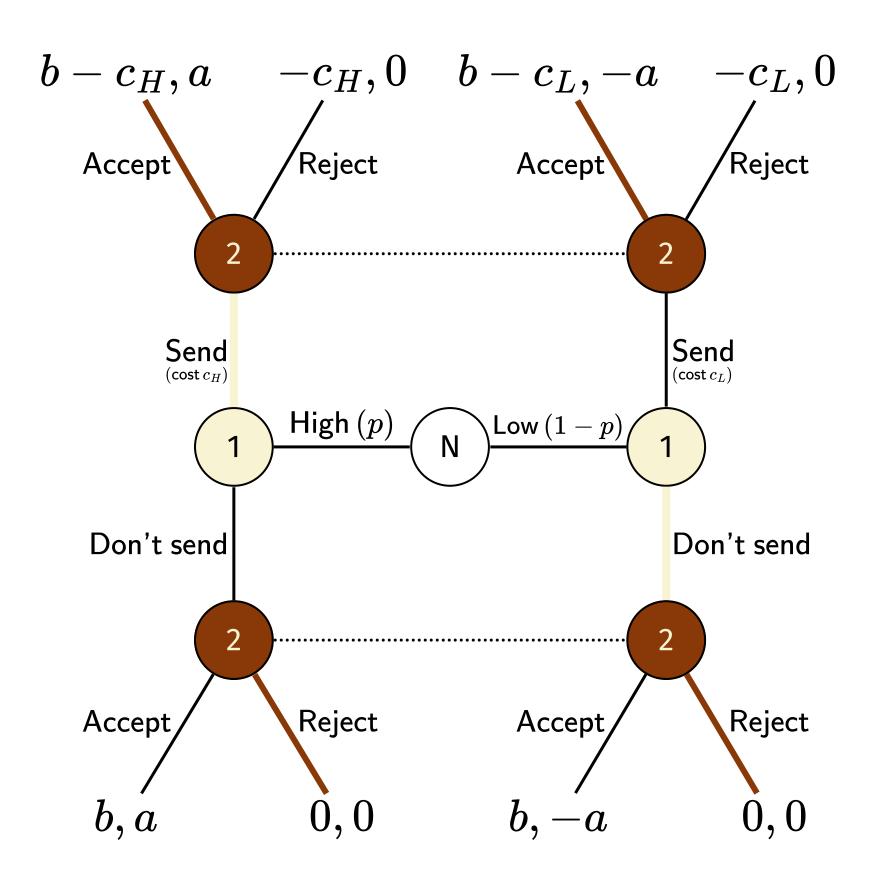
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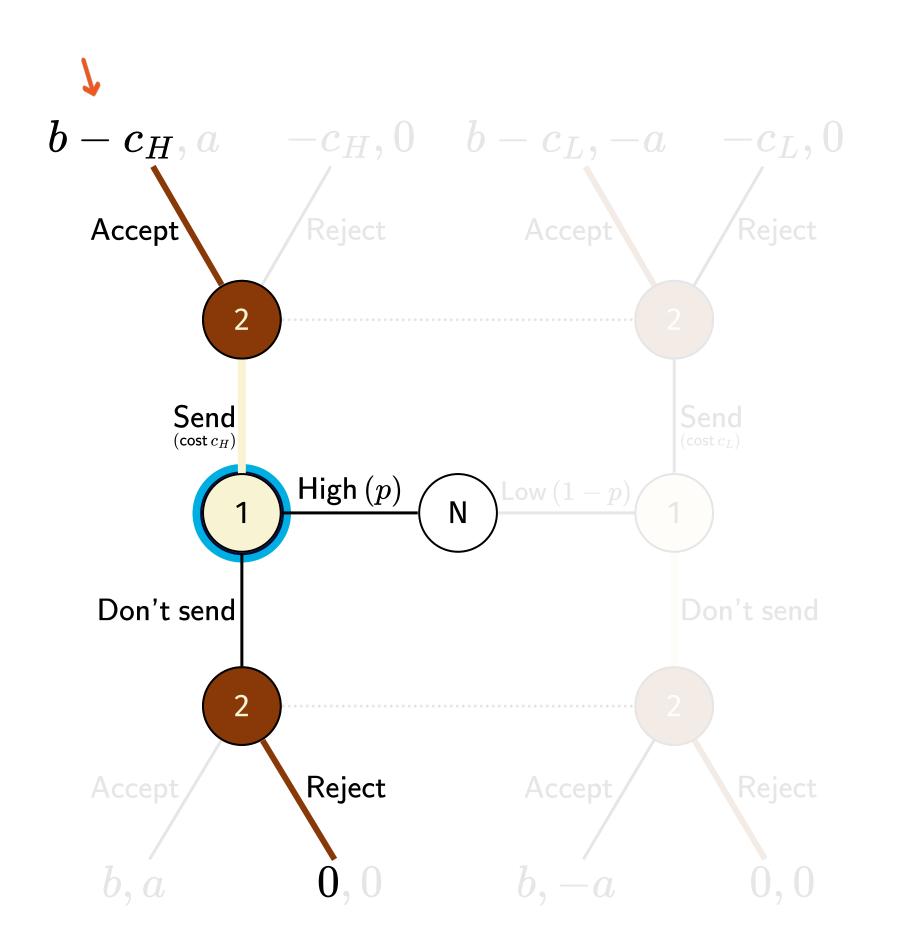
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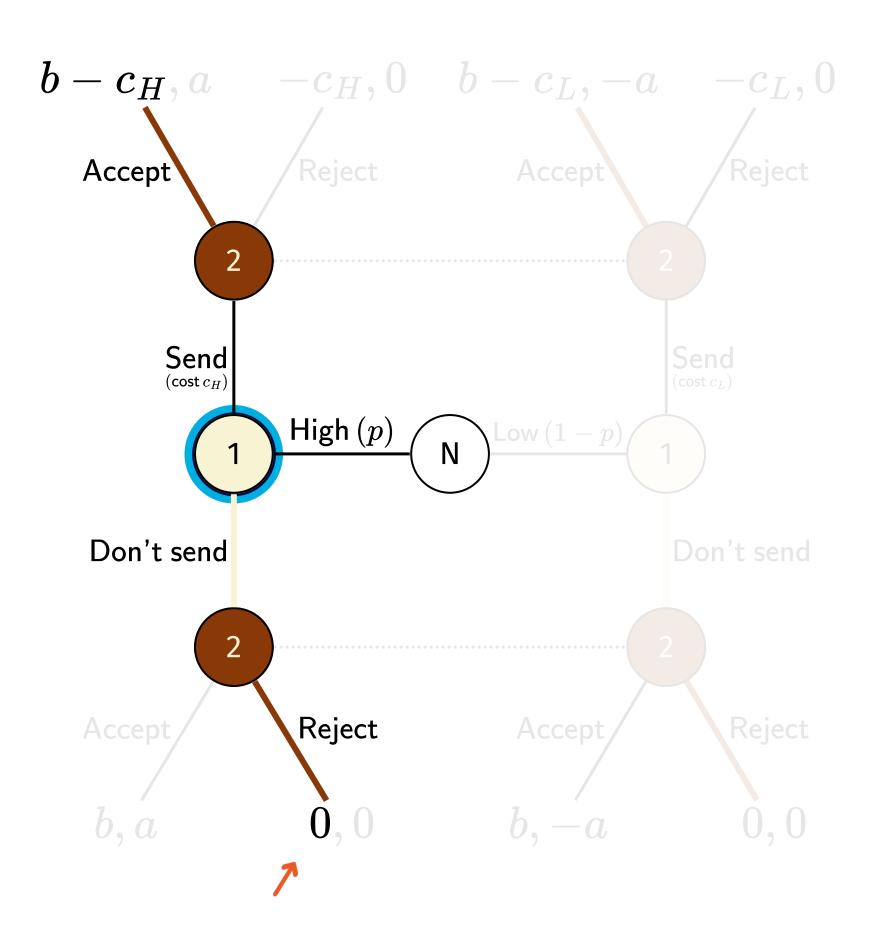
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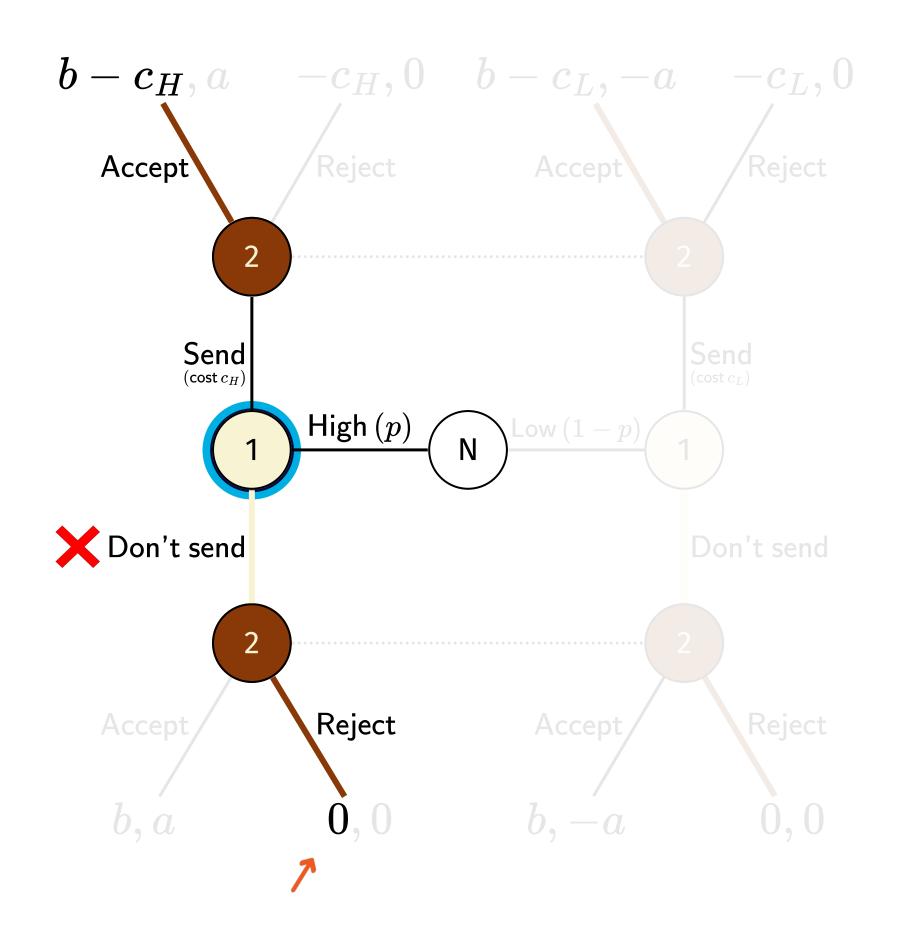


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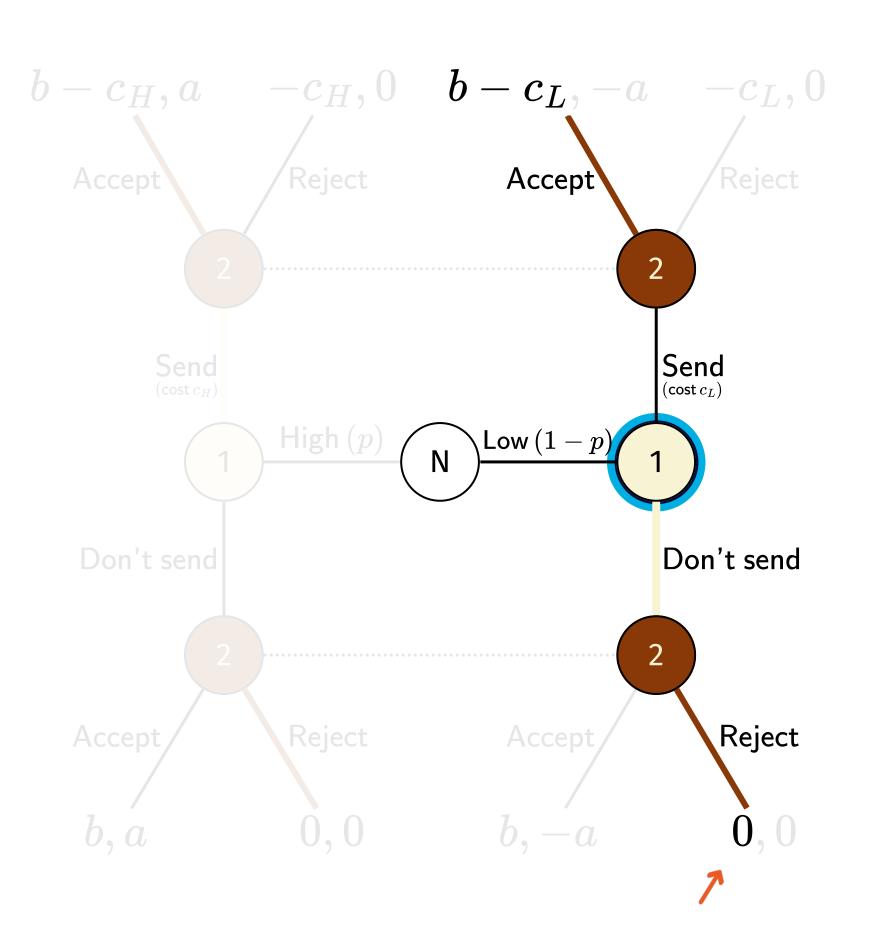


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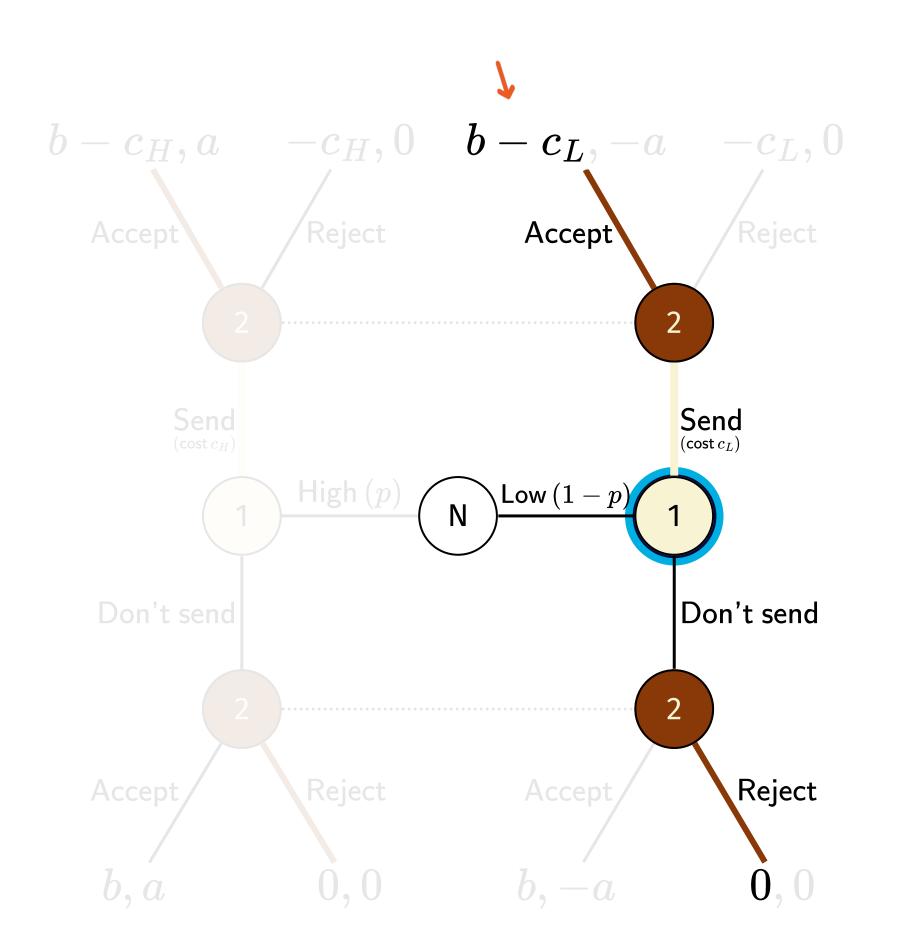


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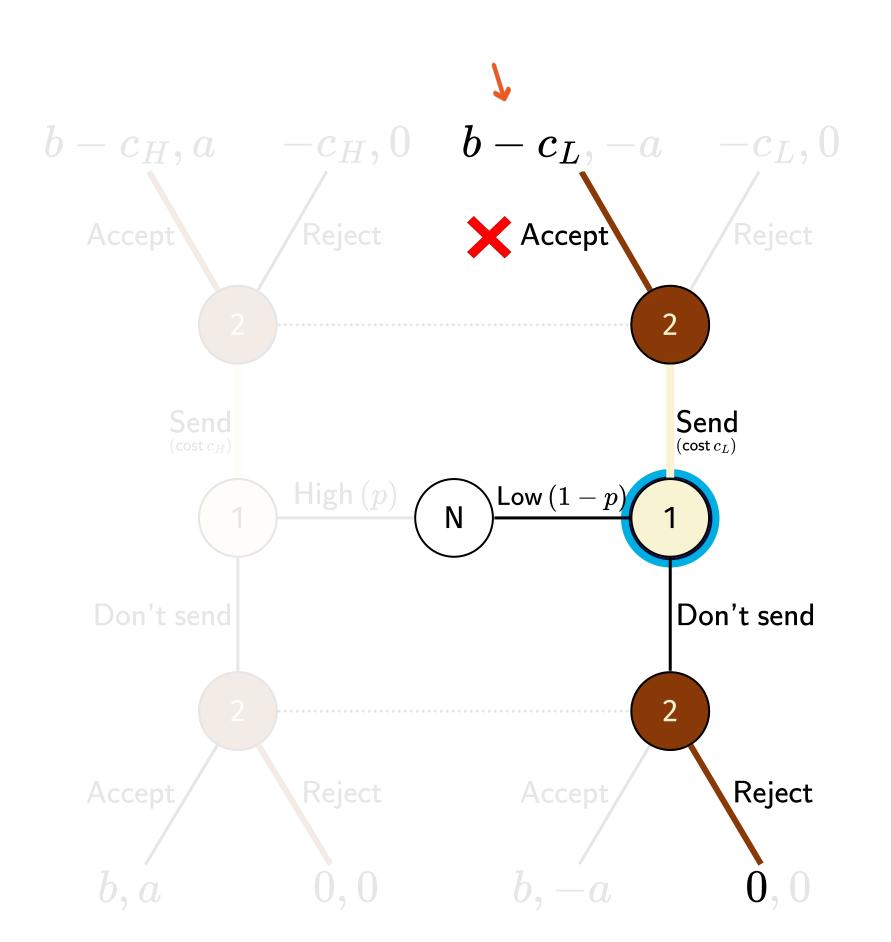


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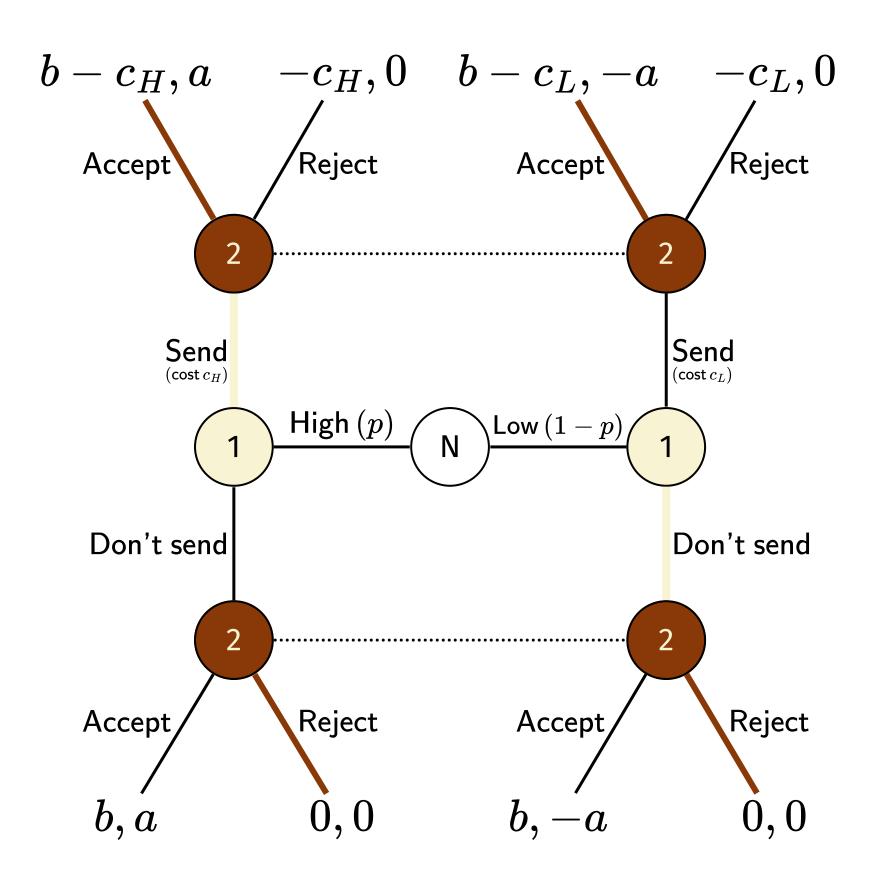
which we've assumed to be the case.

Keeping Player 2's strategy fixed, Player 1 does not want to deviate just in case:

$$b-c_H \geq 0$$
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which is equivalent to:

$$c_H \leq b \leq c_L$$
.



In a separating equilibrium the signal is costly enough that only the high types can afford to send the signal.



In equilibrium, resources are wasted in order to signal one's type.



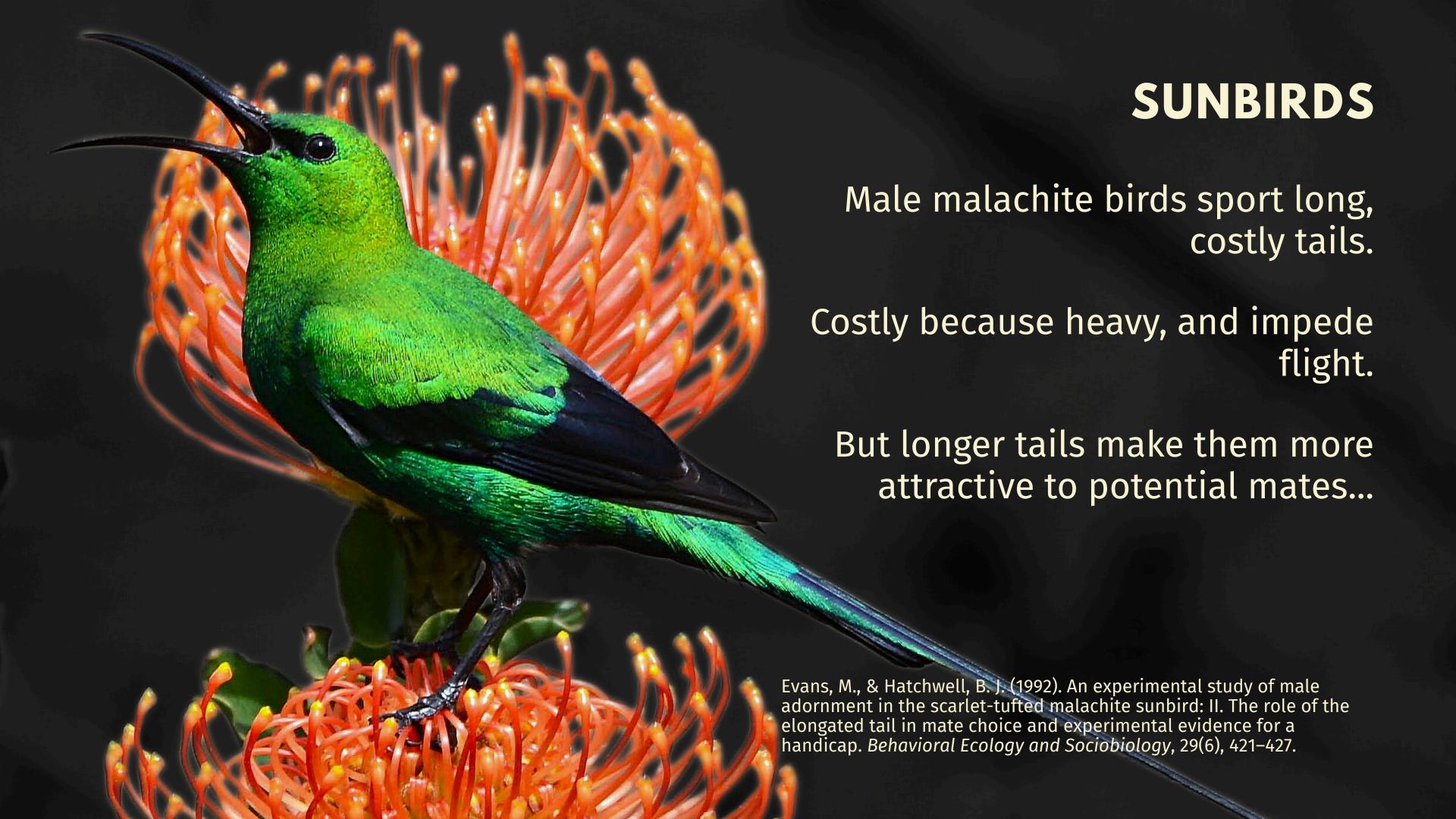
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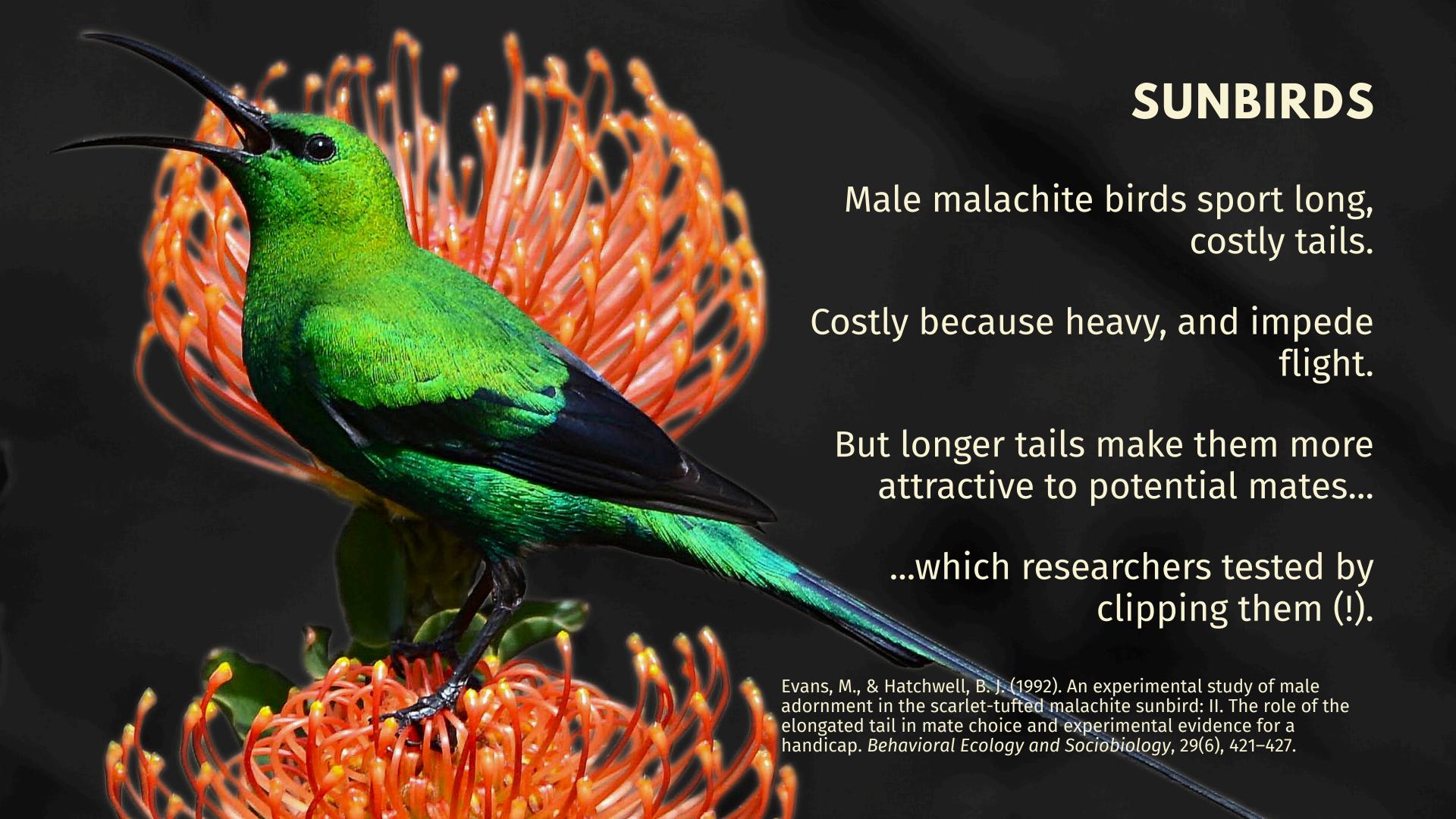
# Crucially, this only happens if the signal is less onerous for the more desirable type.

Yoeli, E., & Hoffman, M. (2022). Hidden Games: The Surprising Power of Game Theory to Explain Irrational Human Behavior. Basic Books.

# Costly signaling shows up everywhere.







Presumably, a costly signal shows that the sender is fit enough to afford it.

## FANCY STUFF



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### **POTLATCHES**

At some Kwakwaka'wakw potlatches the chief would actually *burn* precious resources.



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At some Kwakwaka'wakw potlatches the chief would actually *burn* precious resources.

Presumably as a signal of prestige.

'I can afford to burn what you don't even have.'

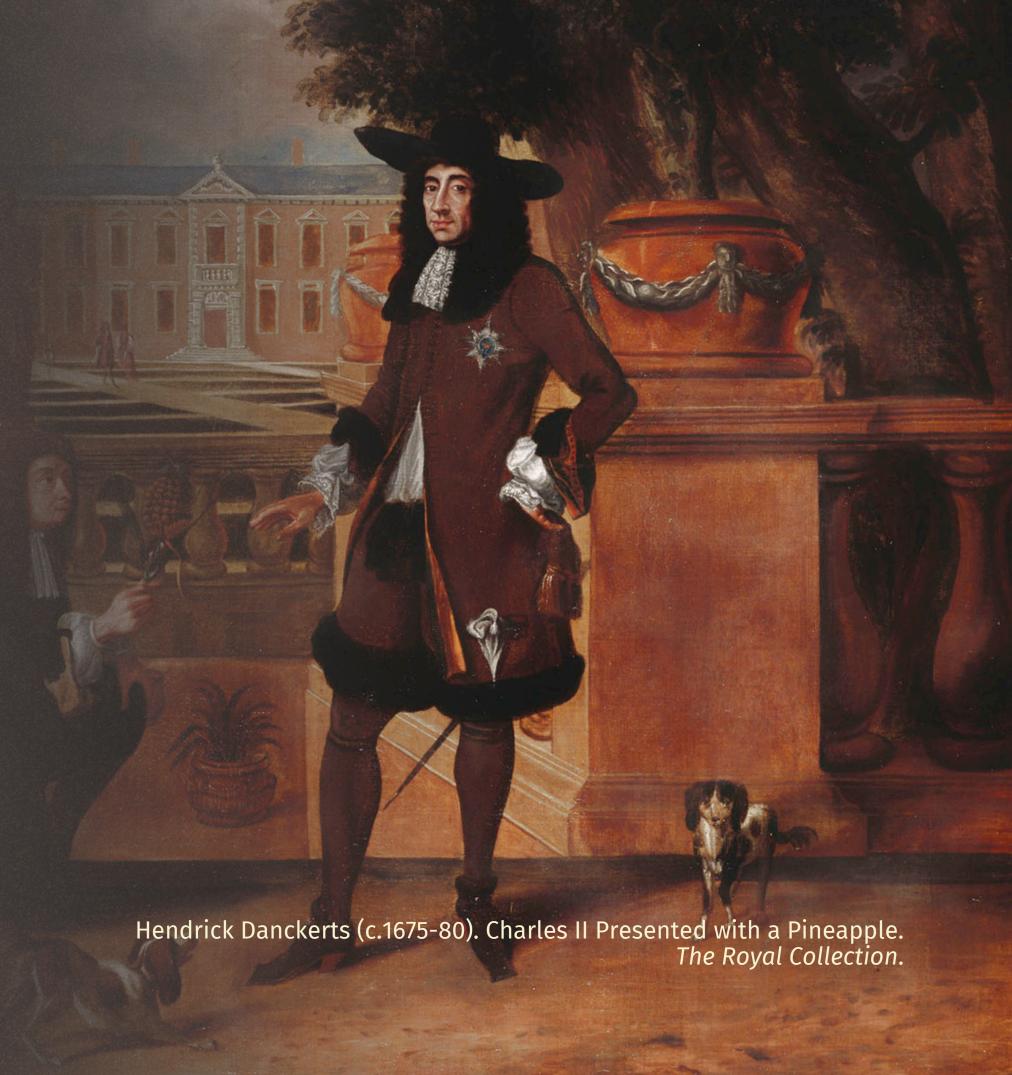






## **PINEAPPLES**

Around the 17<sup>th</sup> - 18<sup>th</sup> centuries, pineapples were an important status symbol.



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Around the 17<sup>th</sup> - 18<sup>th</sup> centuries, pineapples were an important status symbol.

Less impressive today (obviously), when widely available.

Wikipedia contributors. (2025, March 11). <u>Pineapple mania</u>. Wikipedia, Beauman, F. (2005). The pineapple: King of fruits. *Chatto & Windus*.



## **ETIQUETTE**

Knowing the 'proper' rules of conduct signals not just wealth, but also that you have the 'right upbringing.'

Costly, because you need to have been educated into it.



WIRED [@WIRED]. (2024, August 6). <u>Etiquette Expert Answers Etiquette Questions From Twitter | Tech Support | WIRED</u>. Youtube.



Education these days is mostly about signaling.

Signaling that you can jump through the hoops required of a good employee.

Costly? Duh!

Caplan, B. (2018). The Case Against Education: Why the Education System is a Waste of Time and Money. Princeton University Press.



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RICHARD SOSIS

Religious communities have strict rules that their members have to follow.



Signals of how committed you are.

Sosis, R. (2003). Why Aren't We All Hutterites? *Human Nature*, vol. 14, no. 2, pp. 91–127.

## Verse 1

words

**155** 

syllables

214

His palms are sweaty, knees weak, arms are heavy

There's vomit on his sweater already: Mom's spaghetti

He's nervous, but on the surface he looks calm and ready

To drop bombs, but he keeps on forgetting

What he wrote down, the whole crowd goes so loud

He opens his mouth, but the words won't come out

He's choking, how? Everybody's joking now

The clock's run out, time's up, over - blaow!

Snap back to reality, oh, there goes gravity

Oh, there goes Rabbit, he choked, he's so mad but he won't

Give up that easy nope, he won't have it, he knows

His whole back's to these ropes, it don't matter, he's dope

### RAP LYRICS

Complicated rhyming schemes as a signal of cleverness.



Vox [@Vox]. (2016, May 19). Rapping, deconstructed: The best rhymers of all time. Youtube.

More generally, artistic constraints can be interpreted as a way to signal the artist's skill.



But if signals are supposed to show off how cool you are, why do people sometimes bury them?

Why do people say they went to school 'in Boston' when they went to Harvard?



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MOSHE HOFFMAN It's not hard to see.

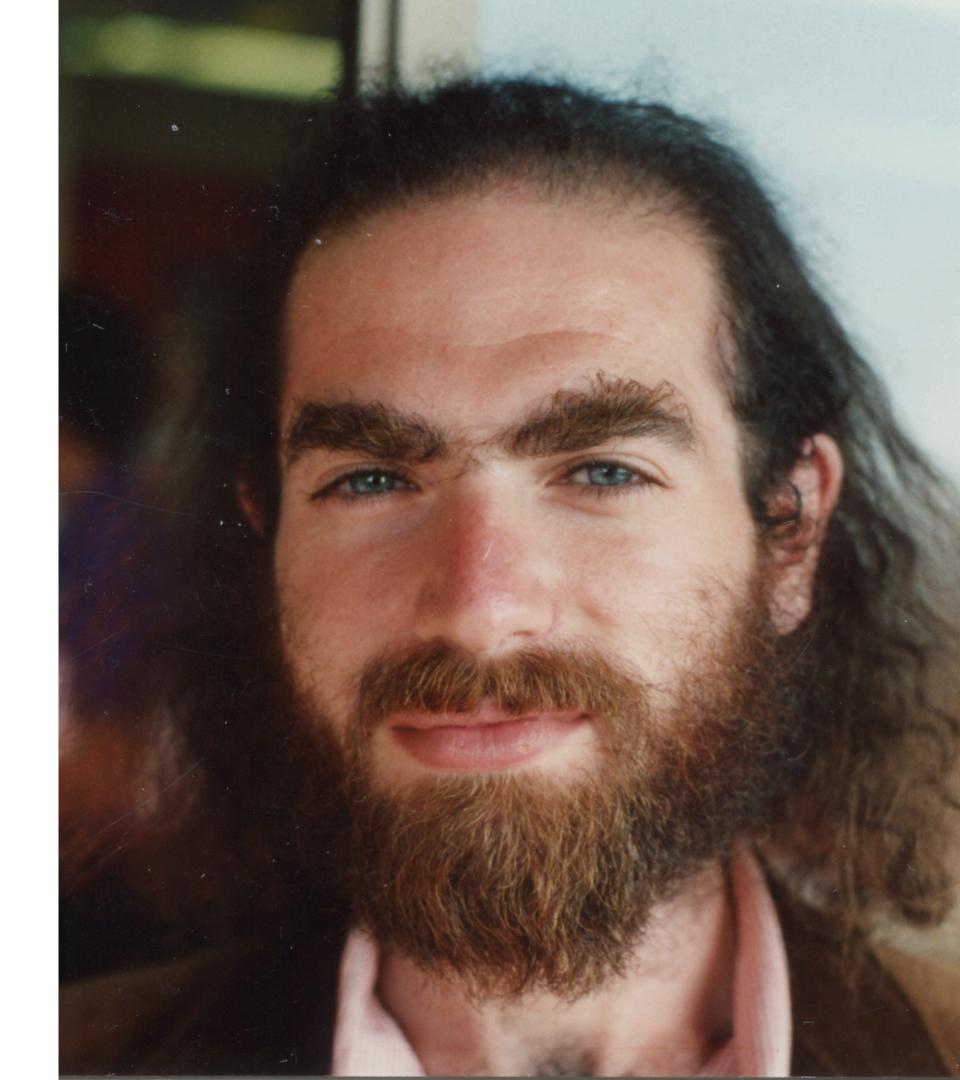


Burying is, itself, a costly signal.

A signal that you can afford for some people to not see your desirable signals.

Hoffman, M., Hilbe, C., & Nowak, M. A. (2018). The signal-burying game can explain why we obscure positive traits and good deeds. *Nature Human Behaviour*, 2(6), 397–404.

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At the same time, he is much more famous having refused the awards than if he'd accepted them.



Pro tip: if you ever get the Nobel prize, refuse it.:)

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#### **SPECIFIC OBSERVERS**

Signals can be meant for a narrow, specialized audience (critics, connoisseurs).