

# INFORMED CHOICES, INCLUSIVE VOICES: EPISTEMIC JOURNEYS IN DEMOCRATIC DECISION MAKING LEARNING FROM OTHERS SOCIAL LEARNING AND INFORMATION CASCADES

May 6, 2024

Adrian Haret a.haret@lmu.de

# Quiz time!

# GDP per capita of Germany, according to recent estimates? 64,600 54,000 44,300

GDP per capita, Purchasing Power Parity, 2022: The average for 2022 based on 19 countries was 34945 U.S. dollars. The highest value was in the USA: 64623 U.S. dollars and the lowest value was in India: 7112 U.S. dollars. The indicator is available from 1990 to 2022. Below is a chart for all countries where data are available.

Measure: U.S. dollars; Source: The World Bank

G20

Countries <b>▲</b> ▼	GDP per capita, PPP, 2022 ▲▼	Global rank ▲▼	Available data 🛦
USA	64623	1	1990 - 2022
Germany	53970	2	1990 - 2022
Australia	51090	3	1990 - 2022
Saudi Arabia	50188	4	1990 - 2022
Canada	49296	5	1990 - 2022
UK	47587	6	1990 - 2022
France	45904	7	1990 - 2022
South Korea	45560	8	1990 - 2022
Italy	44292	9	1990 - 2022
Japan	41838	10	1990 - 2022
Turkey	33150	11	1990 - 2022
Russia	27450	12	1990 - 2022
Argentina	22461	13	1990 - 2022
Mexico	20255	14	1990 - 2022
China	18188	15	1990 - 2022
Brazil	15093	16	1990 - 2022
South Africa	13479	17	1990 - 2022
Indonesia	12410	18	1990 - 2022
India	7112	19	1990 - 2022

## GDP per capita of Germany, according to recent estimates? □ 64,600 ☑ 54,000 □ 44,300

#### ✓ Download data API

# Can social factors make things go awry with collective beliefs?

ODORIC OF PORDENONE In a province of the Grand Can there grow gourds, which, when they are ripe, open, and within them is found a little beast like unto a young lamb...

Odoric of Pordenone [trans. Sir Henry Yule] (2002). The Travels of Friar Odoric. W.B. Eerdmans Publishing Company.



AD 1330

SIR JOHN MANDEVILLE

In Tartary groweth a manner of fruit, as though it were gourds. And when they be ripe, men cut them a-two, and men find within a little beast, in flesh, in bone, and blood, as though it were a little lamb without wool. And men eat both the fruit and the beast. And that is a great marvel.

Of that fruit I have eaten...

and found it wondirfulle.

Mandeville, J. (1900). The Travels of Sir John Mandeville. The Cotton Manuscript in modern spelling. Macmillan and Co. Limited.



AD 1357 - 1371

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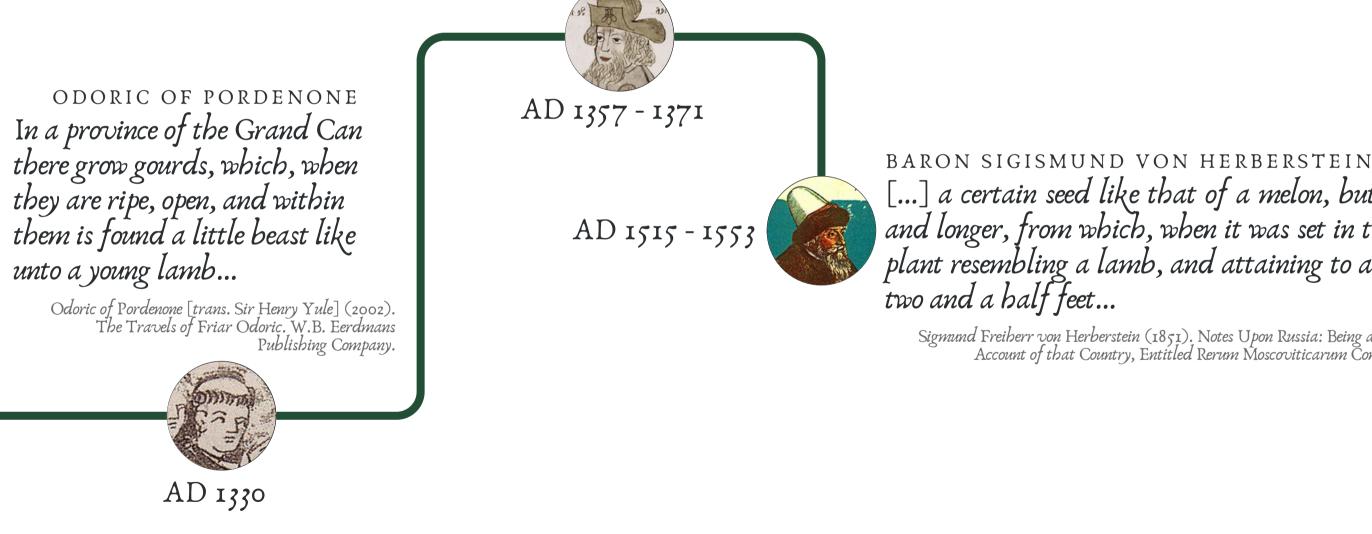
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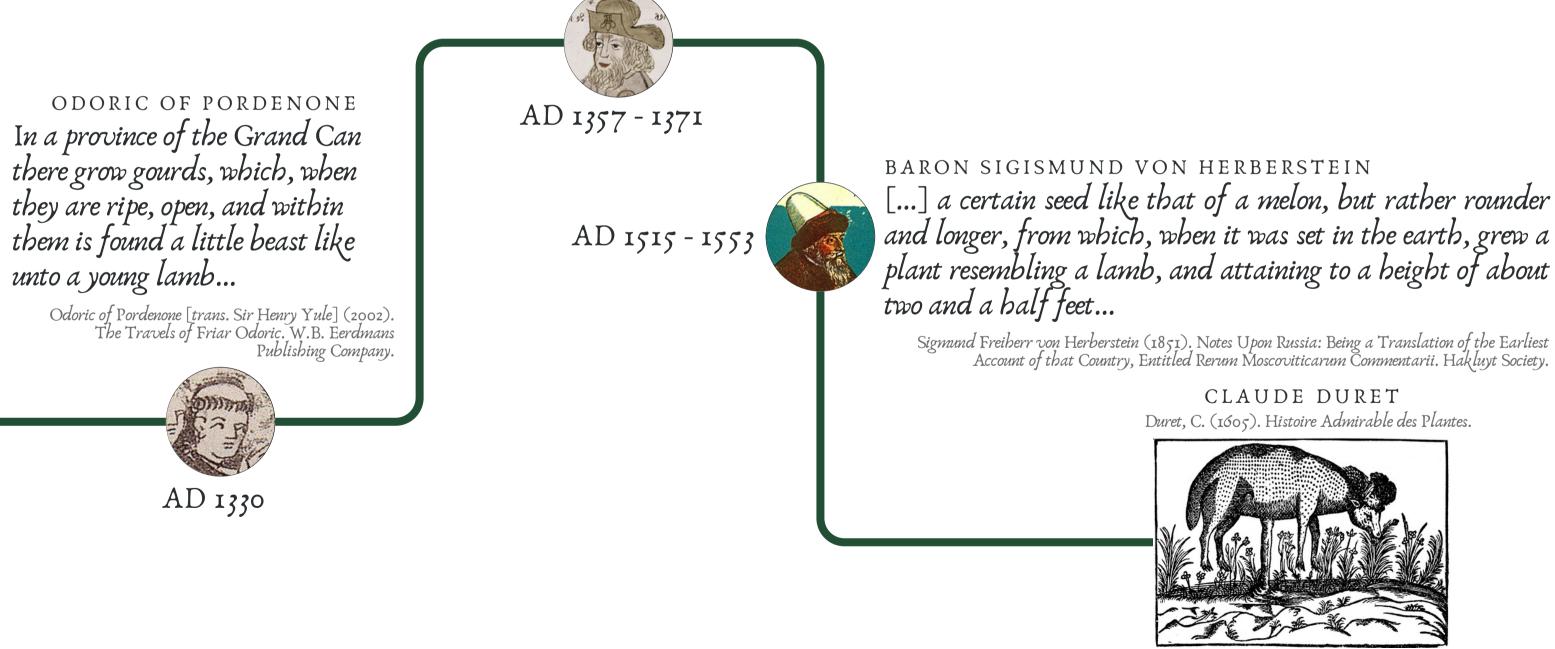
[...] a certain seed like that of a melon, but rather rounder and longer, from which, when it was set in the earth, grew a plant resembling a lamb, and attaining to a height of about

Sigmund Freiherr von Herberstein (1851). Notes Upon Russia: Being a Translation of the Earliest Account of that Country, Entitled Rerum Moscoviticarum Commentarii. Hakluyt Society.

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AD 1605

Of that fruit I have eaten...

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ATHANASIUS KIRCHER [...] we assert that it is a plant. Though its form be that of a quadruped, and the juice beneath its woolly covering be blood which flows if an incision be made in its flesh, these things will not move us. It will be found to be a plant. Kircher, A. (1641). Magnes; sive de arte magneticâ opus tripartitum.

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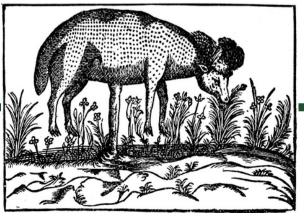
AD 1330

AD 1357 - 1371

AD 1515 - 1553

BARON SIGISMUND VON HERBERSTEIN [...] a certain seed like that of a melon, but rather rounder and longer, from which, when it was set in the earth, grew a plant resembling a lamb, and attaining to a height of about two and a half feet...

Sigmund Freiherr von Herberstein (1851). Notes Upon Russia: Being a Translation of the Earliest Account of that Country, Entitled Rerum Moscoviticarum Commentarii. Hakluyt Society.





AD 1641

CLAUDE DURET Duret, C. (1605). Histoire Admirable des Plantes.

AD 1605

Of that fruit I have eaten...

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ENGELBERT KAEMPFER I have searched ad risum et nauseam for this zoophyte feeding on grass, but have found nothing.

Kaempfer, E. (1712). Amœnitatum Exoticarum politico-physico-medicarum fascicul.



AD 1683

AD 1641

ATHANASIUS KIRCHER [...] we assert that it is a plant. Though its form be that of a quadruped, and the juice beneath its woolly covering be blood which flows if an move us. It will be found to be a plant. Kircher, A. (1641). Magnes; sive de arte magneticâ opus tripartitum.



AD 1605

## Let's model this.



**MORRIS DEGROOT** 

### Agents are represented by nodes in a social network, and update their opinions depending on the opinions of their peers.

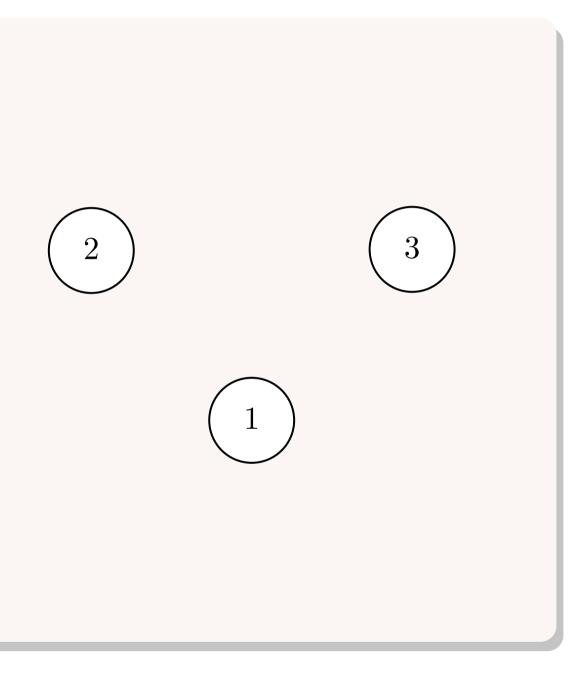
# THE DEGROOT MODEL

agents	$1,2,\ldots,n$
time	$t \in \{0, 1, 2, \dots\}$
belief of agent $i$ at $t$	number between $0$ and $1$
social network	directed graph with agents as ver and who-pays-attention-to-who a
agent i's neighborhood	agents that $i$ pays attention to
weight on edge from $i$ to $j$	number that indicates how much we assume $i$ distributes a total we
update rule	at time $t + 1$ every agent updates to a weighted average over the be

rtices, as edges

n weight *i* places on *j*'s opinion; veight of 1 across *i*'s neighborhood s their belief oeliefs of neighbors

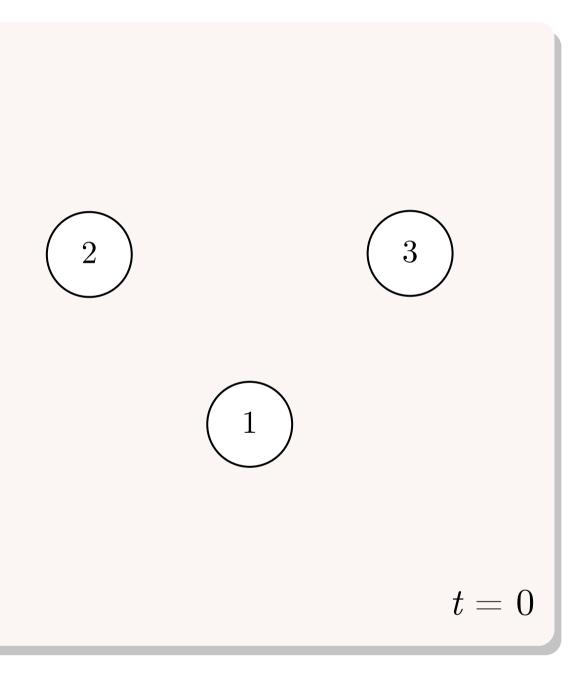
# **Agents** 1, 2, 3



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### Time

 $t=0,\,1,\,2,\,...$ 



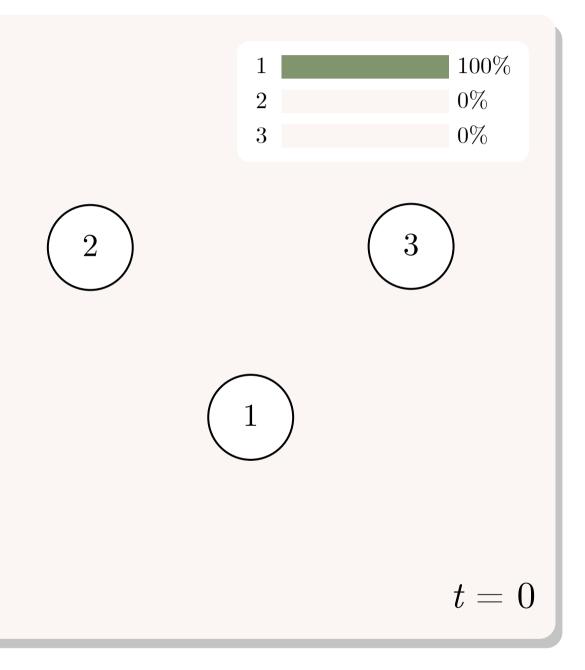
 $1,\,2,\,3$ 

#### Time

 $t=0,\,1,\,2,\,...$ 

#### Beliefs

agent 1 starts out at 0, agent 2 starts out at 0.6, agent 3 starts out at 1



 $1,\,2,\,3$ 

#### Time

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#### Beliefs

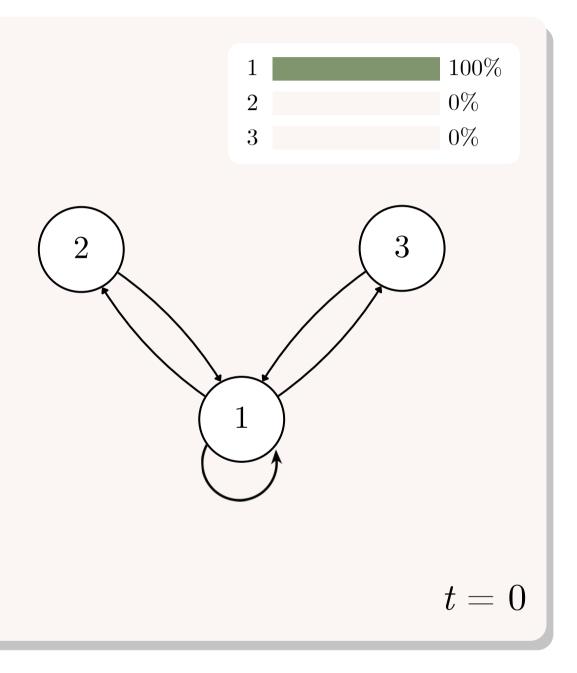
agent 1 starts out at 0, agent 2 starts out at 0.6, agent 3 starts out at 1

#### Social network

1 pays attention to everyone, 2 and 3 pay attention only to 1

### Neighborhoods

1's neighborhood is {1, 2, 3}, etc.



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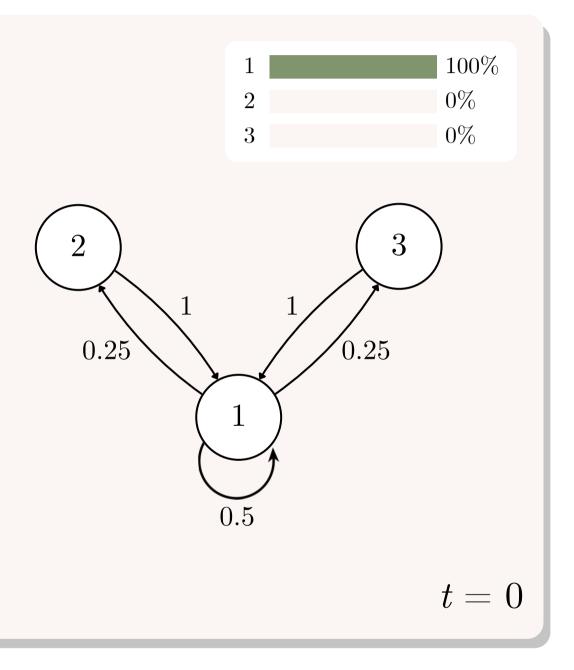
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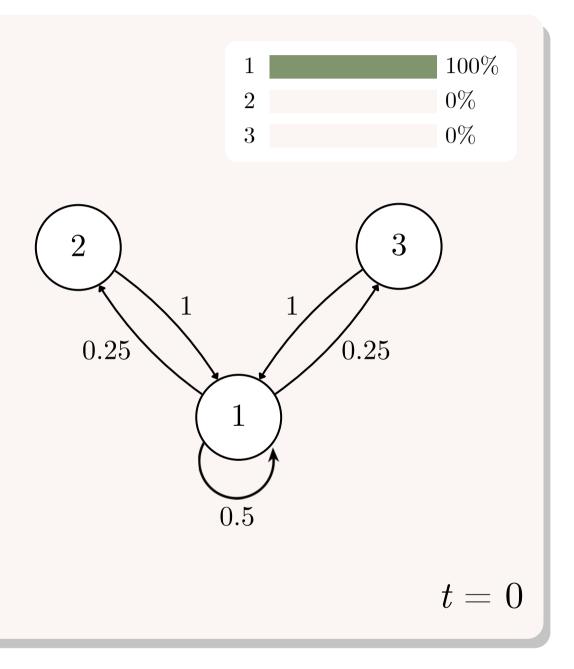
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#### **Belief updates**

at time 1 agent 1's belief becomes:



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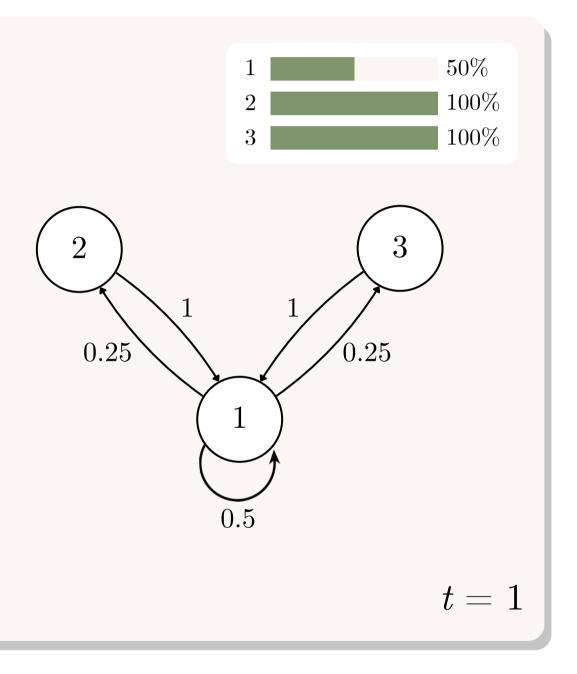
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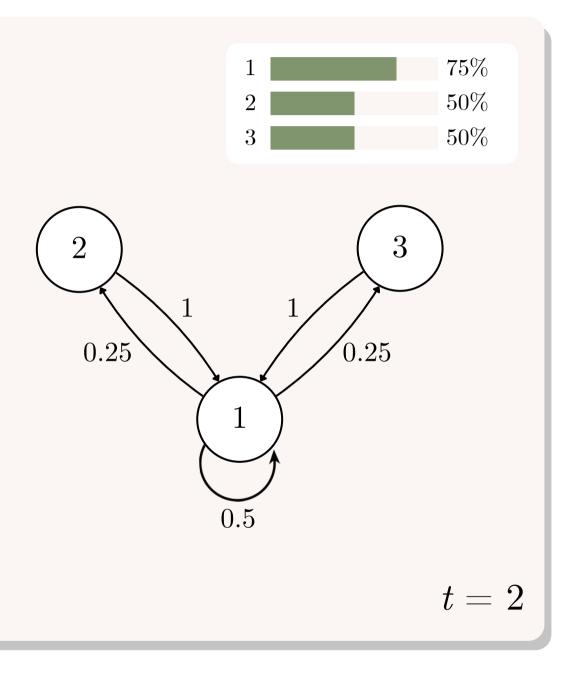
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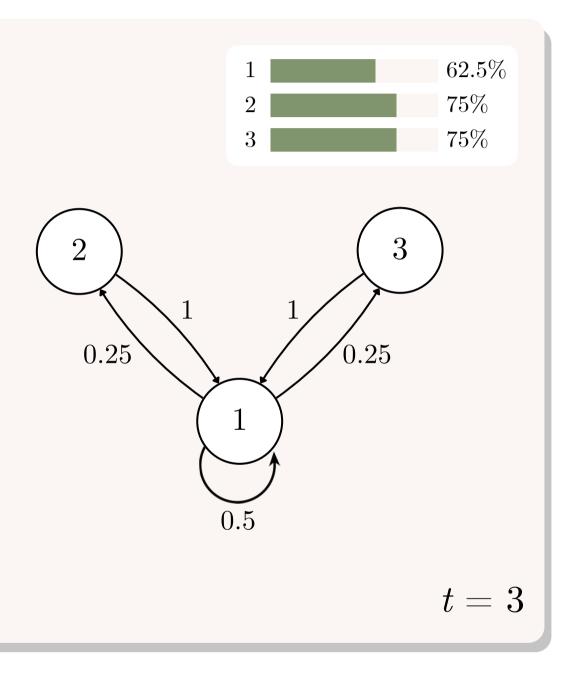
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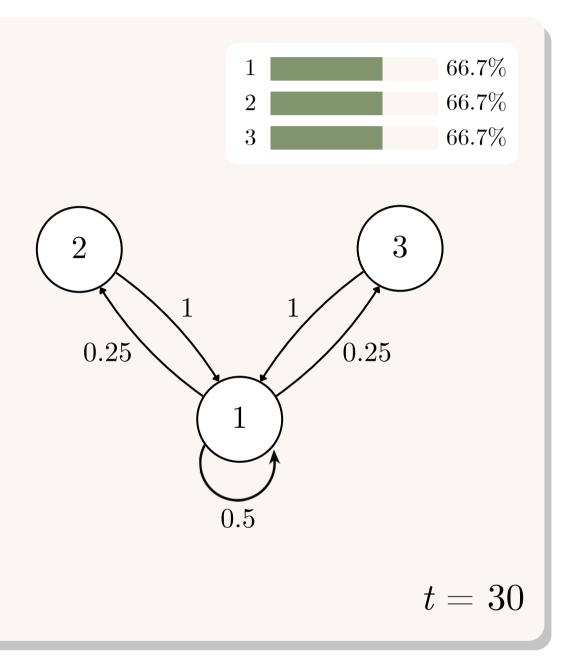
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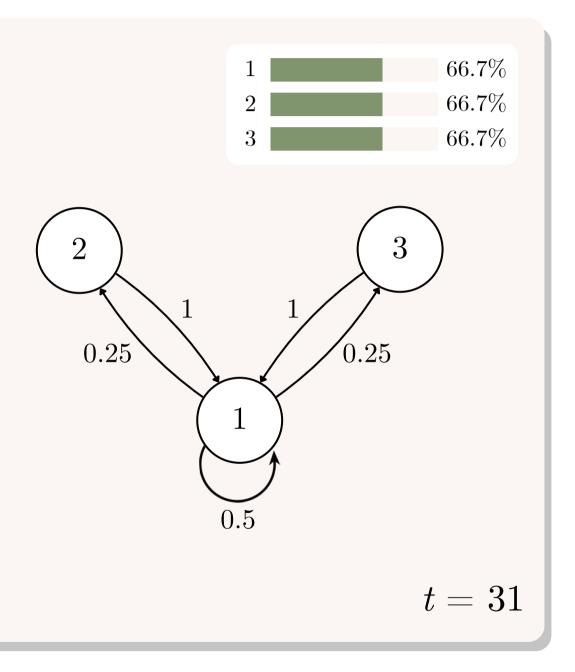
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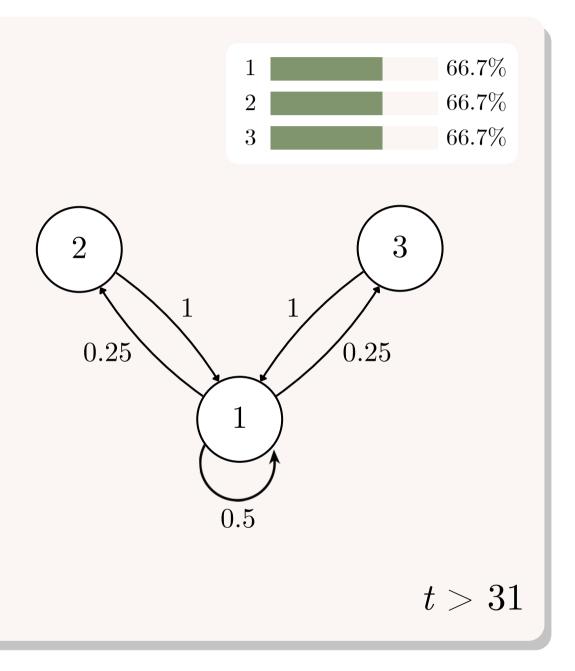
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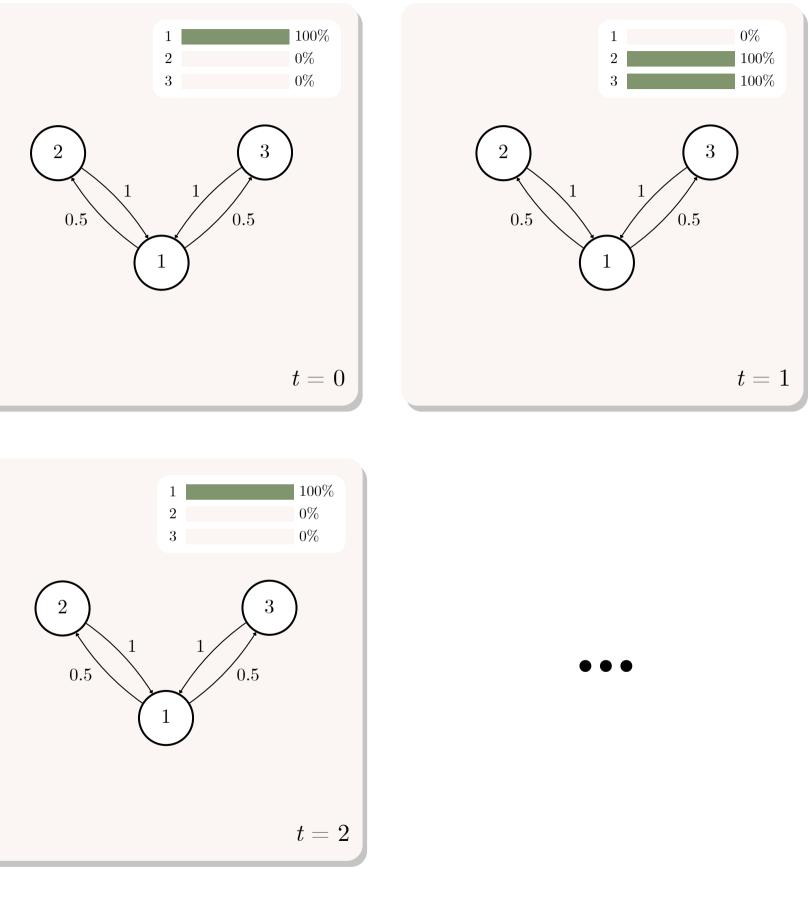
Do the beliefs of each agent converge, i.e., reach a point t after which they do not change anymore?

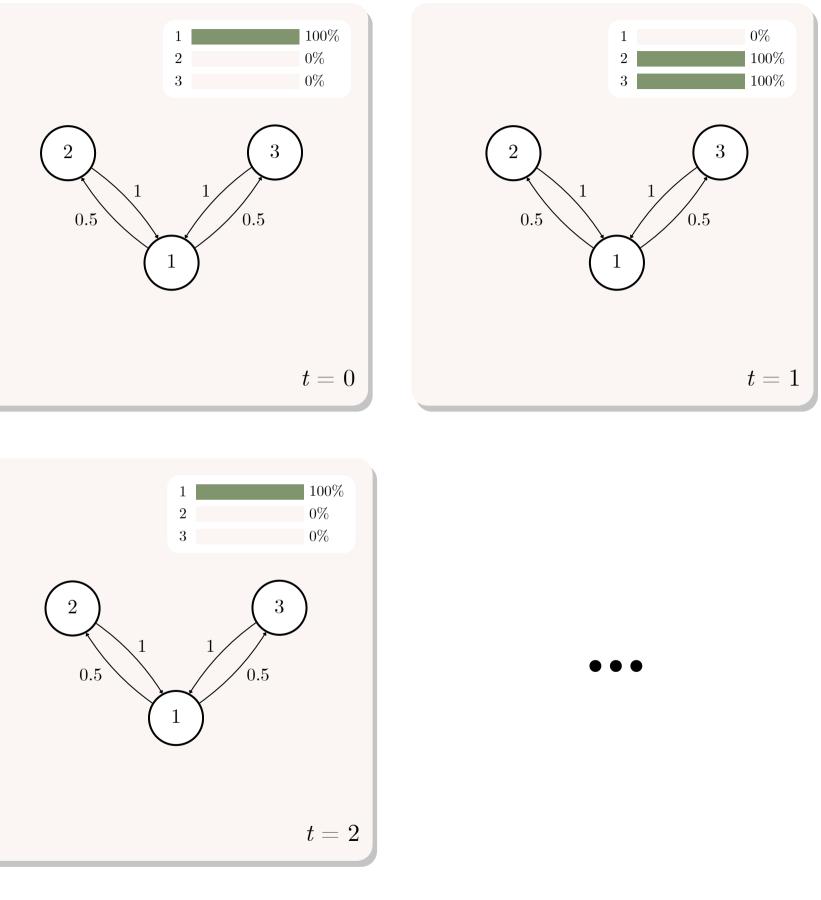
If yes, then is there *consensus*, i.e., do beliefs converge to the same value?



#### MORRIS DEGROOT Yes, under certain conditions!

## Cycles are bad news.







**MORRIS DEGROOT** 

## Ok, then let's just assume there aren't any bad cycles.

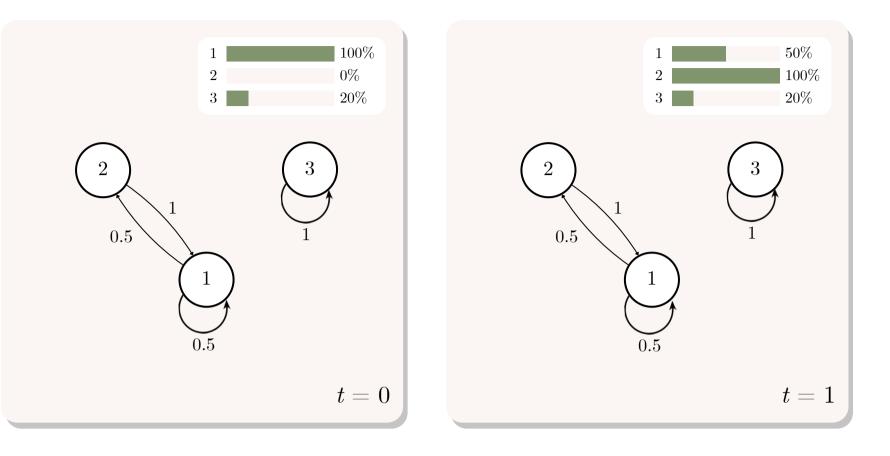
#### DEFINITION

A network is *aperiodic* if the greatest common divisor of any two cycle lengths is 1.



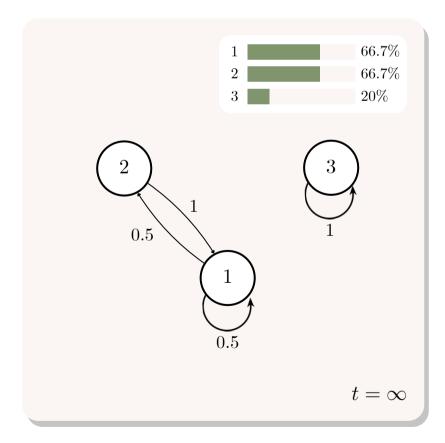
#### **MORRIS DEGROOT** Cycles of lengths 2, 3, 4 are fine.

Cycles of length 2 and 4, or 3 and 6, are not.



# Isolated nodes are also bad news.

. . .





#### **MORRIS DEGROOT** Ok, let's assume there aren't any isolated nodes.

#### DEFINITION

#### A network is strongly connected if there is a path from any node to any other node.



MORRIS DEGROOT

## Aperiodicity and strong connectedness do the trick.

### **THEOREM (DEGROOT, 1974)**

# If the social network is strongly connected and aperiodic, then, for any initial beliefs, agents converge in the limit to the same belief.

DeGroot, M. H. (1974). Reaching a Consensus. Journal of the American Statistical Association, 69(345), 118–121.

# Nice! But what needs to happen for agents in the DeGroot model to arrive at a consensus that is also *correct*?

# THE DEGROOT MODEL WITH TRUTH

$1,2,\ldots,n$
$t \in \{0, 1, 2, \dots\}$
$\mu \in (0,1)$
number between 0 and 1 drawn from a distribution with mea and finite variance above a thresho
aperiodic, strongly connected direction and who-pays-attention-to-who as
agents that $i$ pays attention to
number that indicates how much we assume $i$ distributes a total wei
at time $t + 1$ every agent updates t to a weighted average over the bel

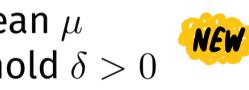
 $\begin{array}{l} \displaystyle \exp \mu \\ \displaystyle \operatorname{old} \delta > 0 \end{array} \end{array}$ 

ected graph with agents as vertices, s edges

weight *i* places on *j*'s opinion; eight of 1 across *i*'s neighborhood their belief eliefs of neighbors

# THE DEGROOT MODEL WITH TRUTH

agents	$1,2,\ldots,n$
time	$t \in \{0, 1, 2, \dots\}$
true state	$\mu \in (0,1)$ NEW
belief of agent $i$ at $t$	number between 0 and 1 drawn from a distribution with mea and finite variance above a thresho
social network	aperiodic, strongly connected direction and who-pays-attention-to-who as
agent i's neighborhood	agents that $i$ pays attention to
weight on edge from $i$ to $j$	number that indicates how much we assume $i$ distributes a total weight
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# BENJAMIN GOLUB We want to speak now of wise *networks*.



### MATTHEW O. JACKSON As with the Condorcet Jury Theorem, this is a limit condition as the network grows larger and larger.

Golub, B., & Jackson, M. O. (2010). Naïve Learning in Social Networks and the Wisdom of Crowds. American Economic Journal: Microeconomics, 2(1), 112–149.





### DEFINITION

We write  $G_n$  for a network with *n* vertices.

A sequence  $G_1, G_2, \ldots, G_n, \ldots$  of (strongly connected and aperiodic) networks of increasing size is wise if the consensus belief approaches the true state  $\mu$  asymptotically, as ngoes to infinity.

### BENJAMIN GOLUB There's a really cool way of thinking about the consensus belief.

Golub, B., & Jackson, M. O. (2010). Naïve Learning in Social Networks and the Wisdom of Crowds. American Economic Journal: Microeconomics, 2(1), 112–149.



# There's a really cool way of thinking about the



### MATTHEW O. JACKSON The consensus belief is a linear combination of the initial beliefs and the *eigenvector centralities* of the nodes.

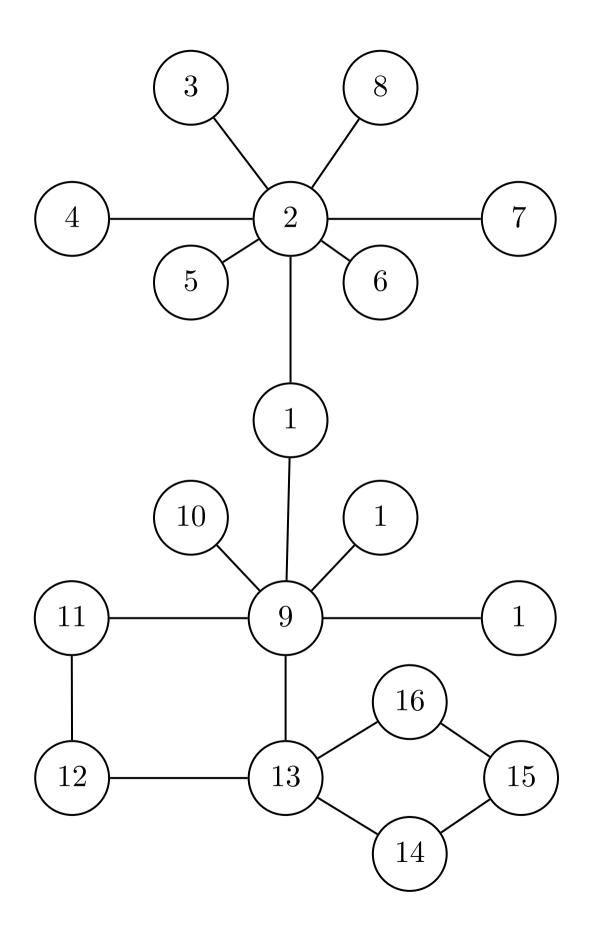
Golub, B., & Jackson, M. O. (2010). Naïve Learning in Social Networks and the Wisdom of Crowds. American Economic Journal: Microeconomics, 2(1), 112–149.

**BENJAMIN GOLUB** consensus belief.



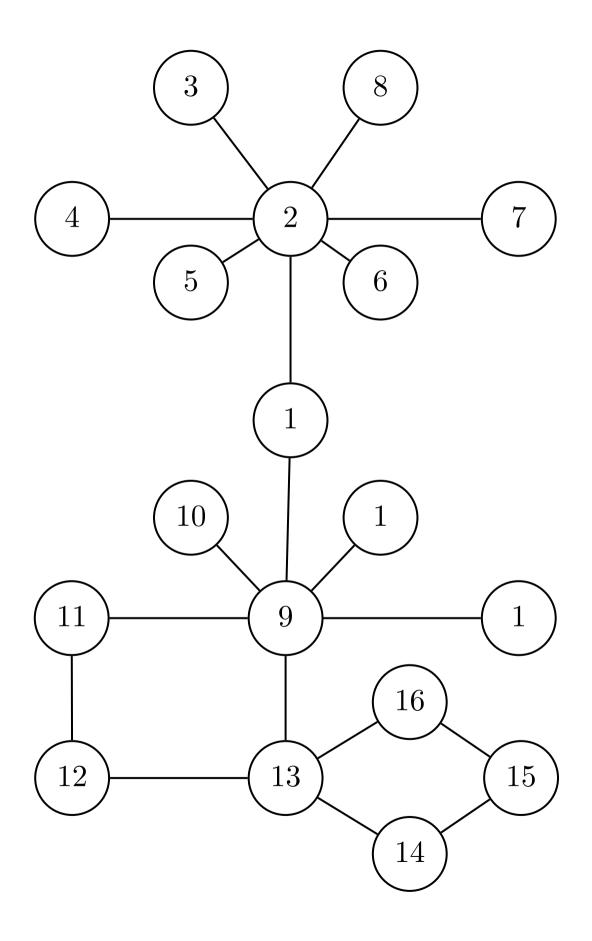
# The *centrality* of a node in a network is a measure of how influential that node is.

A node is influential if it is connected to an influential node.



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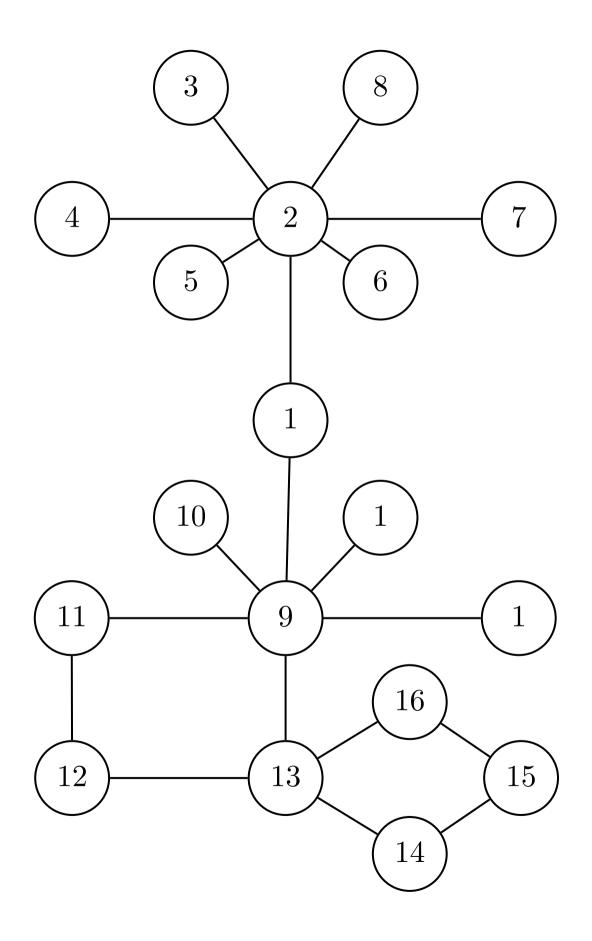
The centrality of a neighbor is proportional to the sum of neighbors' centralities.



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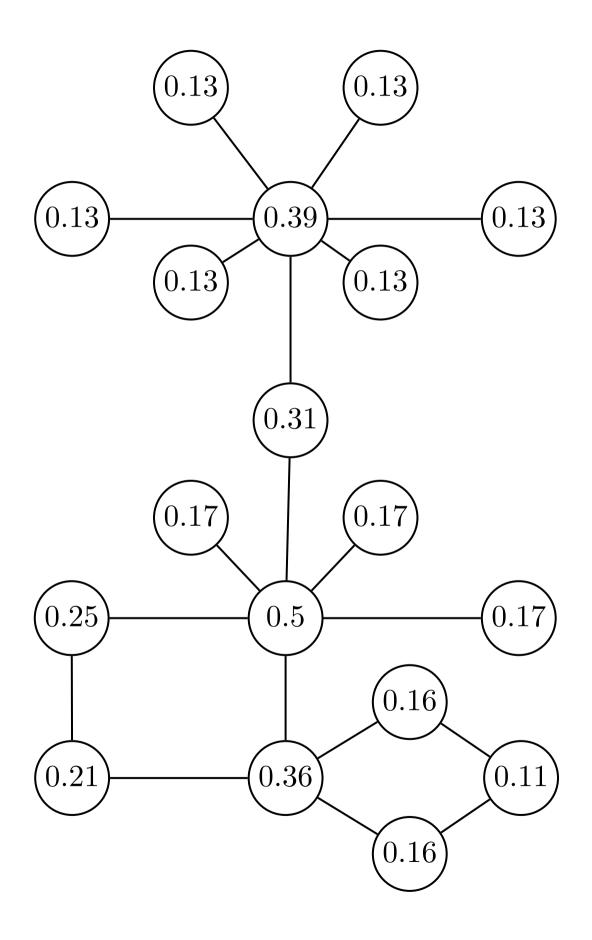
Obtained by solving a system of linear equations.



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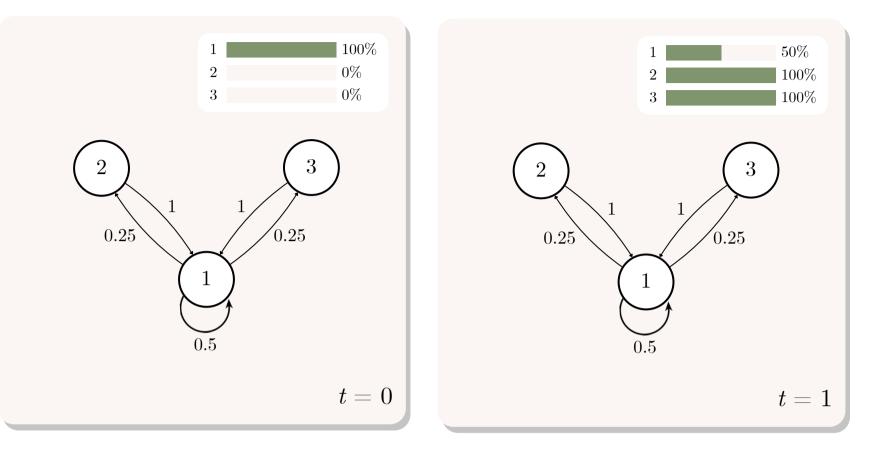






LARRY PAGE SERGEY BRIN

# Eigenvector centrality behind the (original) Google algorithm to rank webpages.

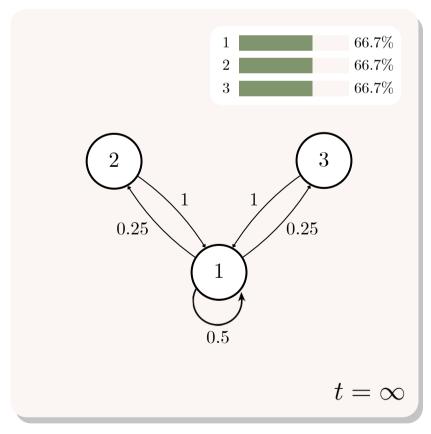


The eigenvector centralities are c = (2/3, 1/6, 1/6).

Centralities indicate the importance of the nodes for the limit consensus belief:

$$\left(\frac{2}{3}, \frac{1}{6}, \frac{1}{6}\right) \cdot (1, 0, 0) = \frac{2}{3} \cdot 1 + \frac{1}{6} \cdot 0 + \frac{1}{6} \cdot 0$$
$$= \frac{2}{3}.$$

. . .



### **THEOREM (GOLUB & JACKSON, 2010)**

A sequence  $G_1, G_2, \ldots, G_n, \ldots$  of (strongly connected and aperiodic) networks of increasing size is wise if and only if the eigenvector centrality of every agent *i* approaches 0 asymptotically, as n goes to infinity.

Golub, B., & Jackson, M. O. (2010). Naïve Learning in Social Networks and the Wisdom of Crowds. American Economic Journal: Microeconomics, 2(1), 112–149.

## For a network to be wise, there can't be a node that, in the long run, retains positive influence.



### MATTHEW O. JACKSON As the network grows and grows, the influence of every node should go to 0.

Golub, B., & Jackson, M. O. (2010). Naïve Learning in Social Networks and the Wisdom of Crowds. American Economic Journal: Microeconomics, 2(1), 112–149.

**BENJAMIN GOLUB** 



## NETWORKS THAT ARE NOT WISE

The network grows by adding agents that listen to the central agent 1.

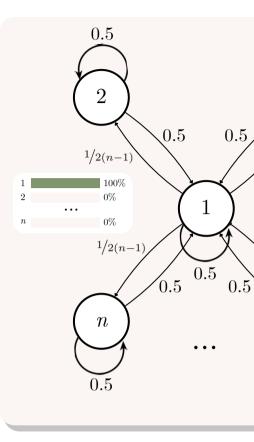
The eigenvector centralities are:

$$c = \left(\frac{1}{2}, \frac{1}{2(n-1)}, \dots, \frac{1}{2(n-1)}\right)$$

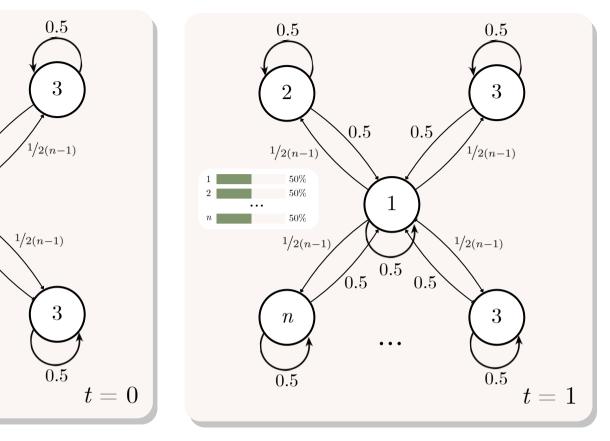
Agent 1 retains a constant share of (network) influence as n grows.

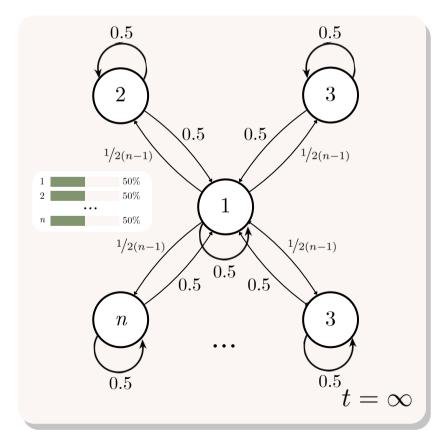
And thus decides the consensus belief.

No bueno.



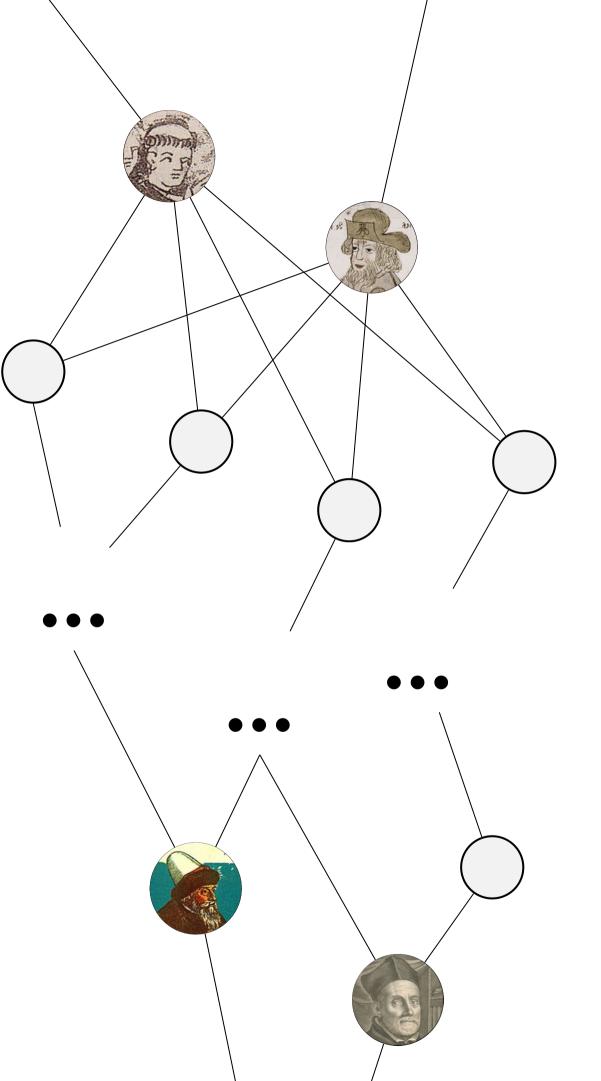
 $\bullet \bullet \bullet$ 





Influential nodes draw the collective opinion towards their own opinion, rather than the truth.

# Maybe what happened with the vegetable lamb...





**ELON MUSK** 

## Free speech is the bedrock of a functioning democracy.

## And [whatever it's called now] is the digital town square where matters vital to the future of humanity are debated.

### But the shape of the social network means that some agents have an outsized influence on collective opinion.

Is this still in line with democratic ideals?



## This can happen even more dramatically in *information cascades*.

Let's try this out!

There's this restaurant you've been dying to try. But you don't know if it's good or bad. You try it once, and also see previous people's reviews. Thumbs up or down?

## One of the most striking regularities of human society is localized conformity.



DAVID HIRSHLEIFER Americans act American, Germans act German...

### **IVO WELCH** We want an explanation of why people conform. Also of why convergence of behavior can be idiosyncratic and fragile.

Bikhchandani, S., Hirshleifer, D., & Welch, I. (1992). A Theory of Fads, Fashion, Custom, and Cultural Change as Informational Cascades. The Journal of Political Economy, 100(5), 992–1026.



### ABHIJIT BANERJEE A common real world example concerns the choice of restaurants.

Banerjee, A. (1992). A Simple Model of Herd Behavior. *The Quarterly Journal of Economics*, 107(3), 797–817.

SUSHIL BIKHCHANDANI





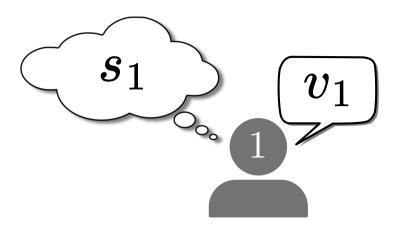
# THE MODEL

agents  $N = \{1, ..., n\}$ true alternative  $\theta \in A$ , we usually assume  $\theta = a$ 

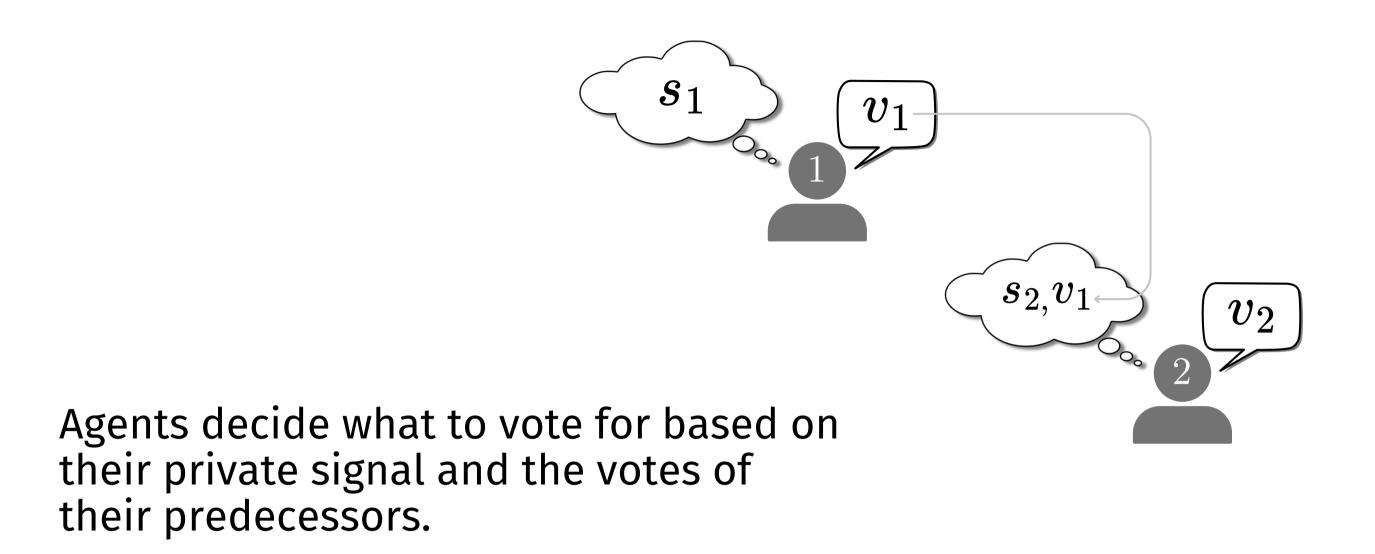
alternatives  $A = \{a, b\}$ voter *i*'s signal  $s_i \in A$ probability of a correct signal i's  $\Pr[s_i = \theta] = p$ , with p > 1agents' prior probabilities  $\Pr[\theta = a] = \Pr[\theta = b] =$ agent *i*'s verdict  $v_i \in A$ 

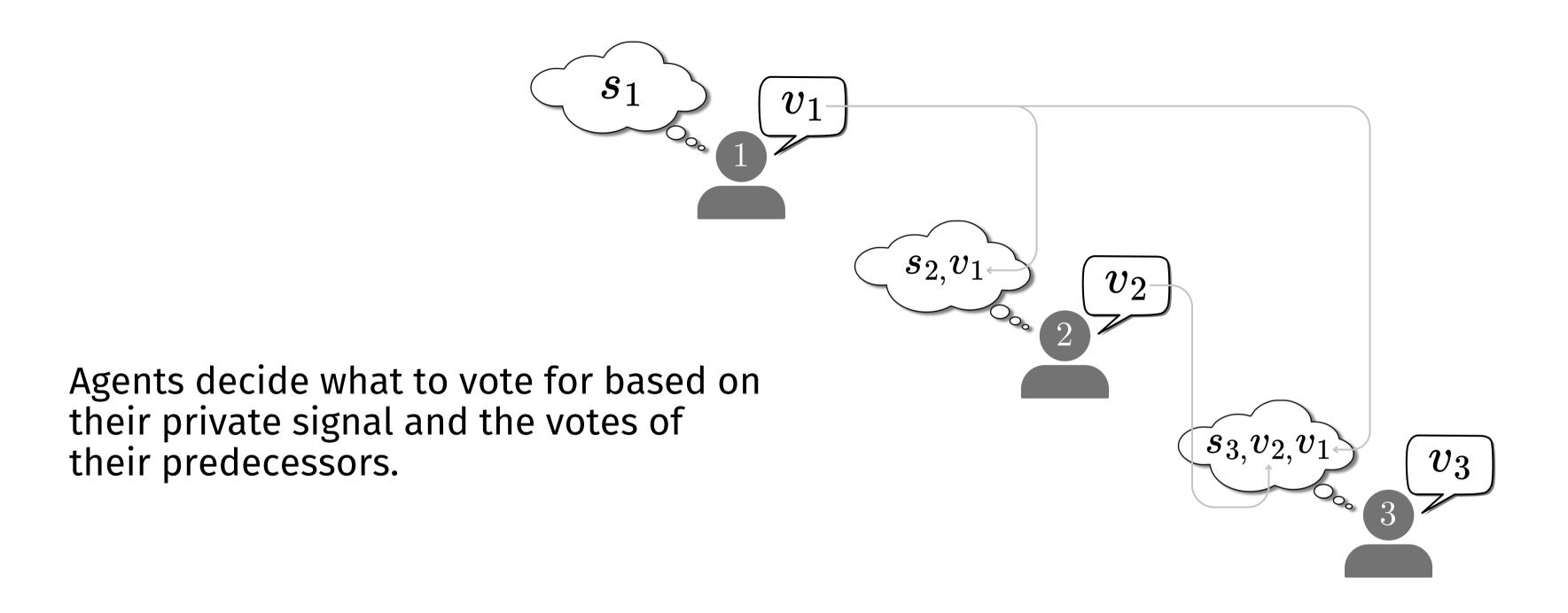
agents speak out in sequence, and see previous verdicts

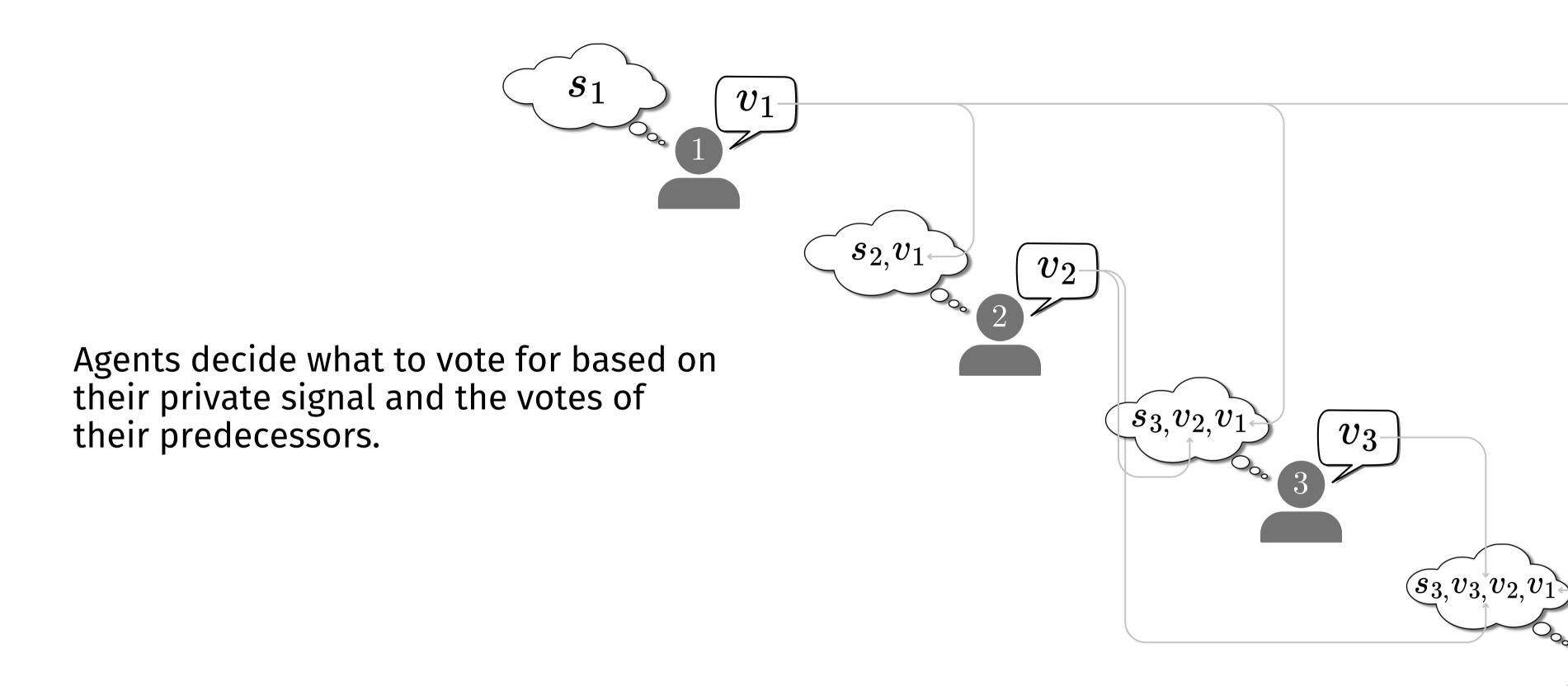
$$\frac{1}{2}$$
  $\frac{1}{2}$ 



### Agents decide what to vote for based on their private signal and the votes of their predecessors.







in what sense optimal?

An informational cascade occurs when it is optimal for an agent, having observed the actions of previous agents, to follow the behavior of the preceding agent without regard to their own information.



### THOMAS BAYES Perforce, they must follow my rule.

# **BAYES' RULE**

We can infer the probability of A given B from the probability of B given A, and the prior probabilities of A and B.

# $\Pr[A|B] = \frac{\Pr[B|A] \cdot \Pr[A]}{\Pr[B]}$

## How do agents decide?

### The (Bayesian) first agent's verdict is determined by their private signal.

 $\Pr\left[\theta = a \mid s_1 = a\right] =$  $\Pr\left[\theta = b \mid s_1 = a\right] =$ 

$$= \frac{\Pr[s_1 = a \mid \theta = a] \cdot \Pr[\theta = a]}{\Pr[s_1 = a]}$$
$$= \frac{\Pr[s_1 = a \mid \theta = b] \cdot \Pr[\theta = b]}{\Pr[s_1 = a]}$$

With p > 1/2, we have that  $\Pr[\theta = a \mid s_1 = a] > \Pr[\theta = b \mid s_1 = a]$ .

The (Bayesian) second agent will vote according to their signal and the previous voter's action.	$\Pr\left[\theta = a \mid a\right]$
If there is a majority for one alternative, the decision reflects that.	$\Pr \left[ \theta = b \mid \right]$ $\Pr \left[ \theta = a \mid \right]$ $\Pr \left[ \theta = a \mid \right]$

If there is a tie, the agent flips a coin.

$$s_{2} = a, v_{1} = a] > \Pr \left[\theta = b \mid s_{2} = a, v_{1} = a\right]$$
  

$$s_{2} = b, v_{1} = b] > \Pr \left[\theta = a \mid s_{2} = b, v_{1} = b\right]$$
  

$$s_{2} = a, v_{1} = b] = \Pr \left[\theta = b \mid s_{2} = a, v_{1} = b\right]$$
  

$$s_{2} = b, v_{1} = a] = \Pr \left[\theta = b \mid s_{2} = b, v_{1} = a\right].$$

The (Bayesian) third agent will go with the trend defined by the first two agents, if there is one.

 $\Pr\left[\theta = b \mid s_3 = b, v_2 = v_1 = b\right] > \Pr\left[\theta = a \mid s_3 = b, v_2 = v_1 = b\right]$ 

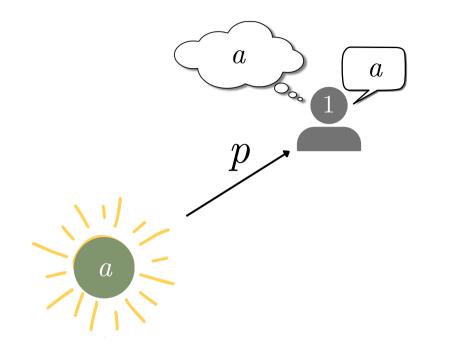
The (Bayesian) third agent will go with the trend defined by the first two agents, if there is one.

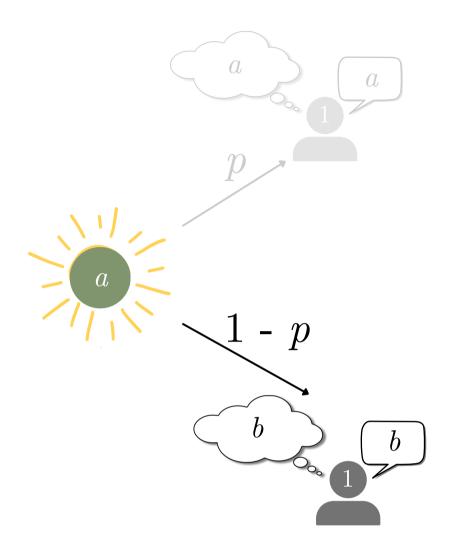
Regardless of their own private signal!

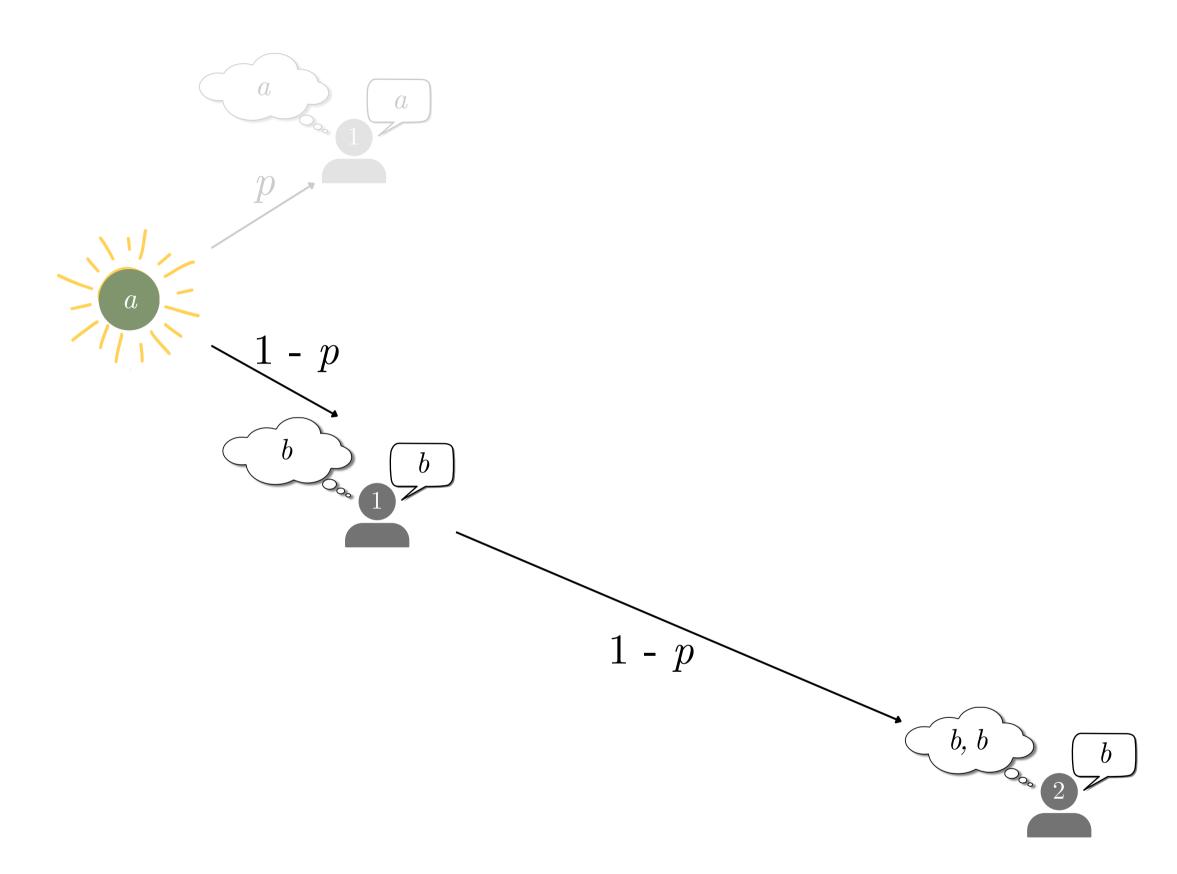
 $\Pr \left[ \theta = b \mid s_3 = b, v_2 \right]$  $\Pr \left[ \theta = b \mid s_3 = a, v_2 \right]$ 

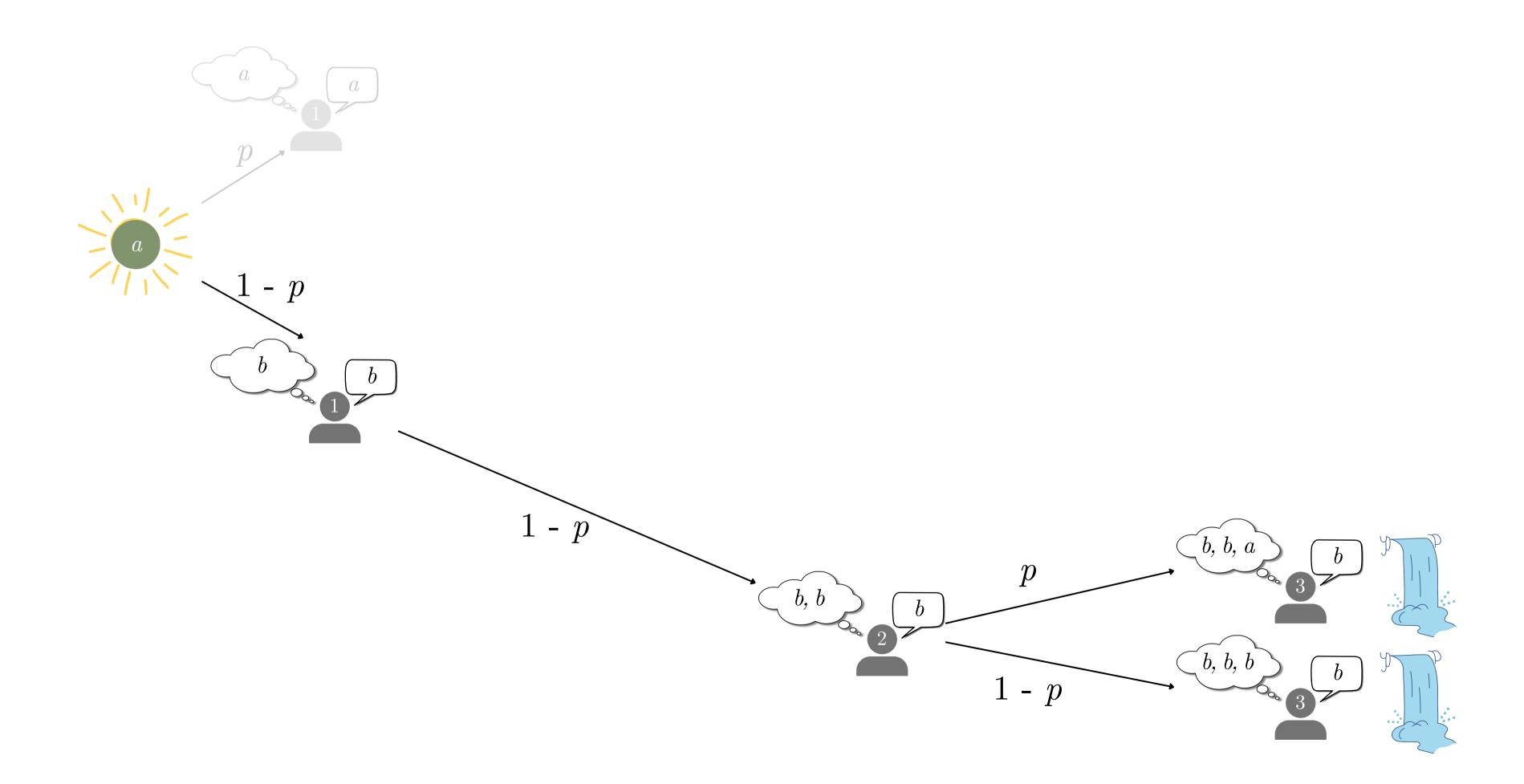
A cascade!

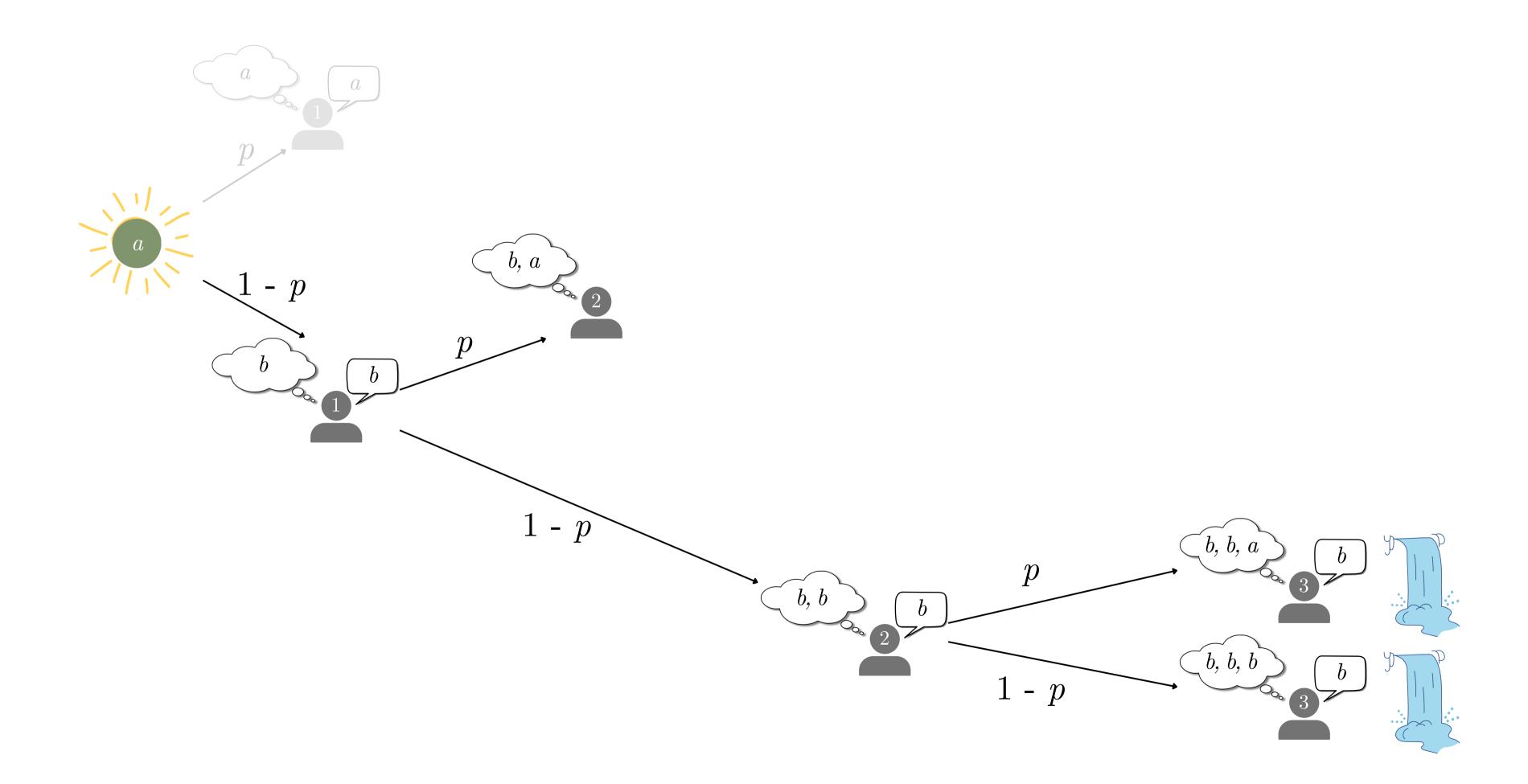
$$v_2 = v_1 = b$$
] > Pr [ $\theta = a \mid s_3 = b, v_2 = v_1 = b$ ]  
 $v_2 = v_1 = b$ ] > Pr [ $\theta = a \mid s_3 = a, v_2 = v_1 = b$ ]

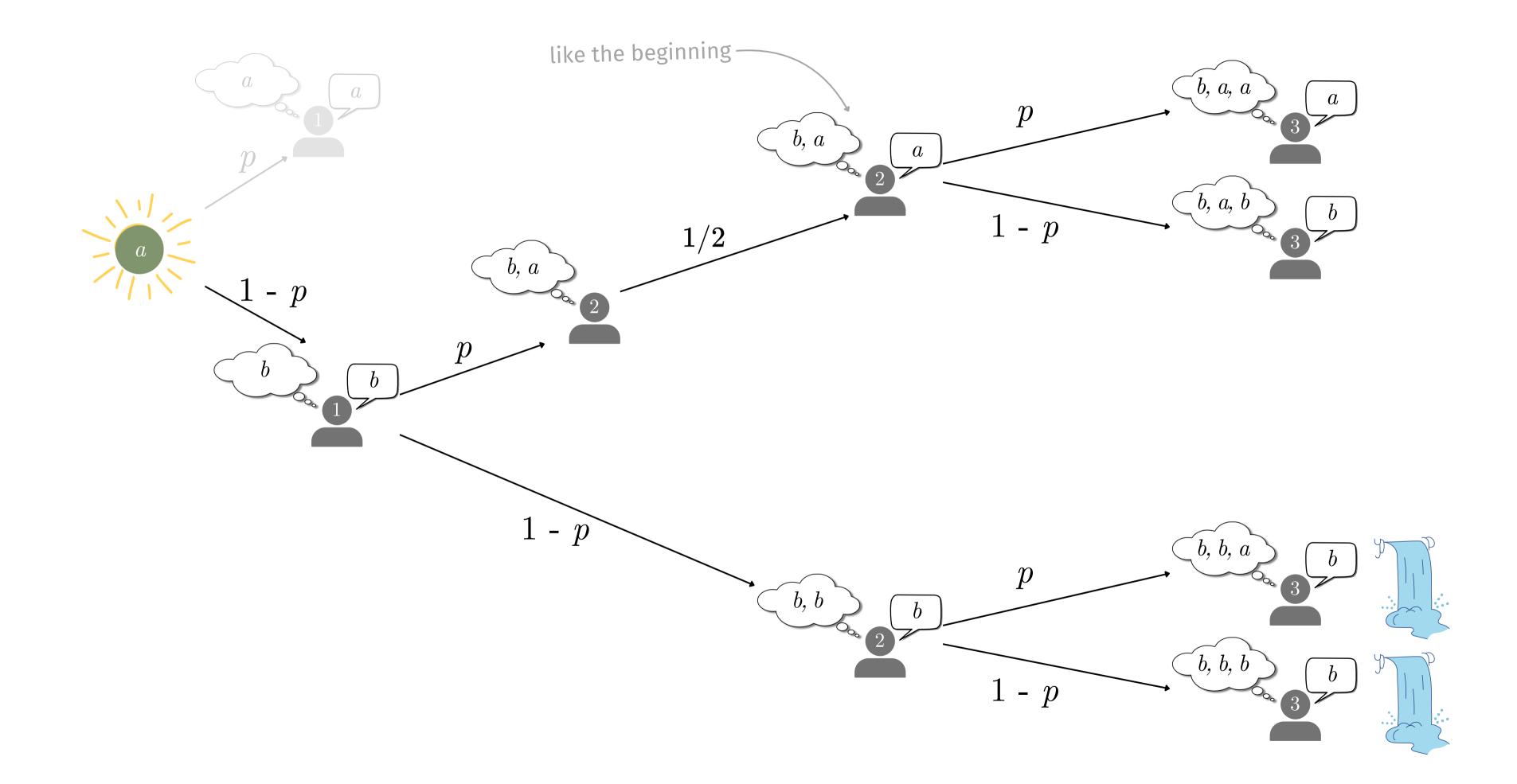


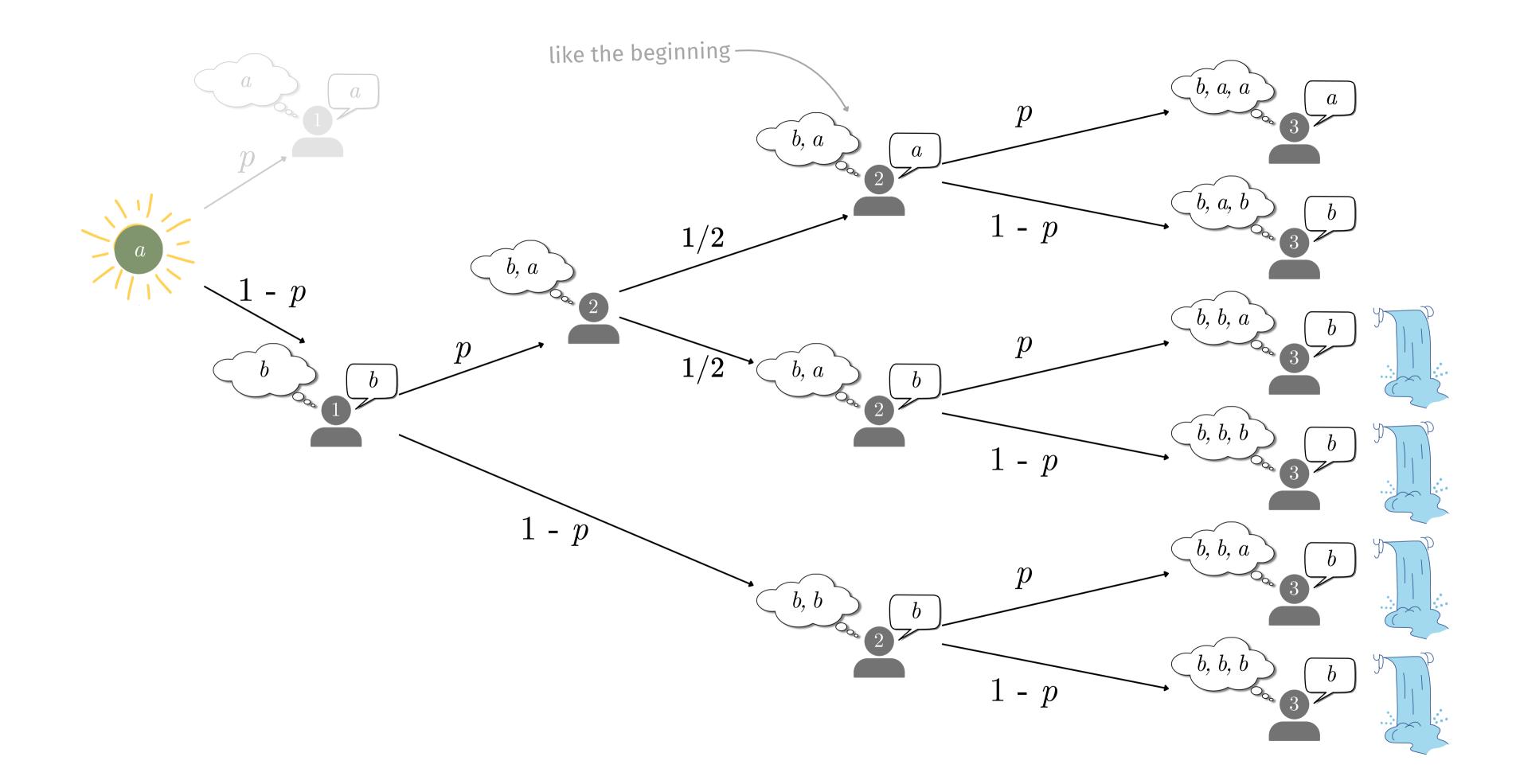




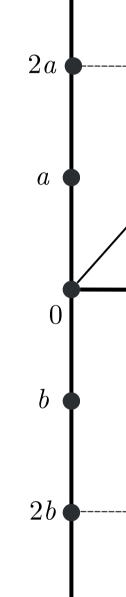


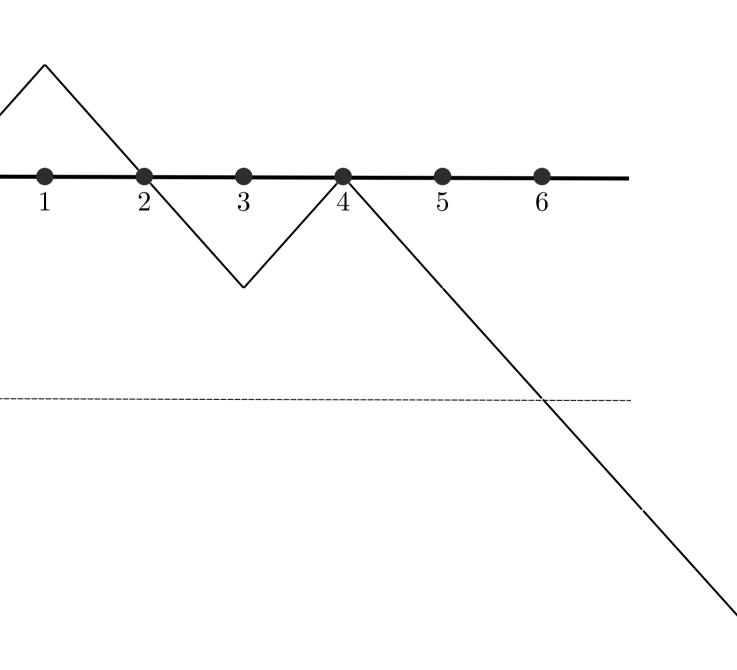






### In general, a cascade occurs as soon as two consecutive agents take the same action.





For large *n*, we are sure to fall into a cascade.



DAVID HIRSHLEIFER The cascade can be for the correct alternative, or for the wrong one.

### **IVO WELCH** Cascades are also fragile, i.e., sensitive to the release of public information.

Bikhchandani, S., Hirshleifer, D., & Welch, I. (1992). A Theory of Fads, Fashion, Custom, and Cultural Change as Informational Cascades. The Journal of Political Economy, 100(5), 992–1026.

# SUSHIL BIKHCHANDANI





Let's sum up.

### Wisdom of crowds is a fragile phenomenon, and it can break down in the presence of strong correlation between voters.



### HÉLÈNE LANDEMORE At the same time, there is more and more evidence that certain forms of communication, e.g., deliberation, are good for decision making.

Landemore, H. (2020). Open Democracy: Reinventing Popular Rule for the Twenty-First Century. Princeton University Press.

CONDORCET



## Can we find better insights, for more realistic scenarios?